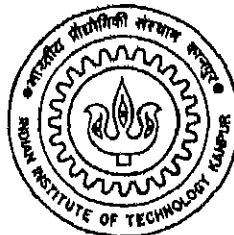# PLANNING AND DESIGN OF NATIONAL COMMAND COMPLEX

by

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DEPARTMENT OF CIVIL ENGINEERING

INDIAN INSTITUTE OF TECHNOLOGY KANPUR

APRIL, 1995

PLANNING AND DESIGN OF NATIONAL COMMAND COMPLEX

A Thesis Submitted
in Partial Fulfillment of the Requirements
for the Degree of

MASTER OF TECHNOLOGY

by

Capt Sanjay Sharma

to the
DEPARTMENT OF CIVIL ENGINEERING
INDIAN INSTITUTE OF TECHNOLOGY KANPUR
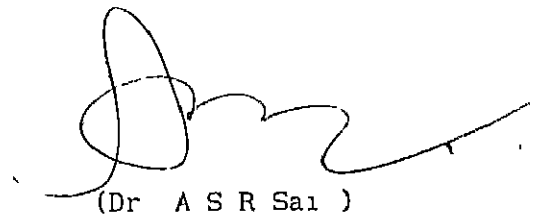**April,1995**

CE-1995-M-SHA-PLA

Dedicated

to

My parents and wife

CERTIFICATE

It is certified that the work contained in the thesis entitled, " PLANNING DESIGN OF NATIONAL COMMAND COMPLEX ", has been carried out by Capt Sanjay Sharma under my supervision and this work has not been submitted elsewhere for the award of a degree.

(Dr A S R Sai)

Professor

Department of Civil Engineering

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Last but not the least, I am indebted to my wife Abha and my daughter Palak for their suffering due to my absence from home for most of the time.

<div align="right">Sanjay</div>

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SYMBOLS

A_f	Area of the facility
A_{cl}	Area of Complex
A_h	Average Projected Area of Human Being
$B(x)$	Buildup Factor
C	Compression Wave Velocity of the Concrete
CEP_e	Circular Error Probability in Locating the Attacker's Aim Point
CEP_r	Circular Error Probability of the Warhead Delivery with Respect to a known Aim Point
C_L	Compression Wave Velocity of the Soil
C_o	Ambient Sound Speed
D	Thickness of the Roof
DOB	Depth of Burial
$erfc$	Error Function
E	Modulus of Elasticity of Concrete
E_{tot}	Fraction of Total Energy in the Form of Thermal Energy
f_{perm}	Permissible Buckling Stress in Cylindrical Shell
$F(t)$	Force at any Time t
F_{cr}	Critical Stress
F_e	Cube Strength
I	Photon Intensity
J	Energy Radiated per unit Area
k	Air Absorption Coefficient
K_o	Coefficient of Earth Pressure
L	Span of the Structure
L_r	Radius Defined by the Attacker for its Successful Mission

M_x, M_y and M_{xy}	Bending Moments in shells
N	Number of Delivery
P(e)	Probability of Explosion
P_o	Ambient Pressure
P_{ovr}	Soil Over Burden Pressure
P_{perm}	Permissible Stress in Spherical Shell
P_q	Stress Applied at the Top of the Structure
P_s	Peak Over Pressure
P_{so}	Ground Surface Over Pressure
Q	Total Thermal Energy Received at any Distance D
QF	Quality Factor
R	Weapon Strike Distance
S_o	Strength of the Weapon Source
t_{max}	Maximum Time for Thermal Pulse
T	Transmittance
T_x, T_y and T_{xy}	Membrane Stresses in shells
U	Shock Front Velocity
v(t)	Velocity of the Structure
w	Deflection along Z axis
W	Weapon Yield
W_h	Average Weight of Human Being
x	Thickness of the Shield
Y_L	Lower Yield Value
Y_U	Upper yield Value
α	Thermal Diffusivity of the Soil
ϵ	Emissivity of the Soil
ϕ	Particle Flux Density
μ	Linear Attenuation Coefficient

ν	Poisson's Ratio
ρ	Density of Soil
σ	Stefan Boltzman Constant
$\sigma_b(t)$	Stress Acting on the Base at any time t
$\sigma_{ff}(t)$	Incident Stress Wave
$\sigma_r(t)$	Stress Acting on the Roof at any time t
$\sigma_s(t)$	Stress Acting on the Side at any time t

ABSTRACT

The planning, layout and design of **National Command Complex** to resist all the nuclear weapon effects, to safeguard our political and military leaders in event of nuclear war has been illustrated

An attempt has been made to combat the adverse effects of weapon by using Reinforced Cement Concrete as a basic construction material. The soil cover on top of the complex is used to mitigate the radiation effects.

An algorithm to design such a specialized specialised structure been suggested. A concealed and dispersed layout of the complex has been chosen to reduce the chances of success of the attacker's mission.

The parametric studies have been performed to obtain the optimal depth of burial from blast, nuclear and thermal radiation considerations for various ranges of explosion.

Static and dynamic analysis have been performed for one of the principal module of the complex using Structural Analysis Program - IV. The results are compared and a design force has been suggested.

Finally, the module has been designed using Indian Standard Codes of Practice and checked for buckling stresses and critical moments

CHAPTER - I

INTRODUCTION

1.1 General

Throughout the history man has sought to protect himself from hostile forces of his environment   Apart from providing shelter from natural danger he has also striven to provide shelters from military threats. Seen historically, the need for defence and improvements in the means of defence were responses to threats and to counter-improvements in the method of attack

1.2 Philosophy of Warfare

From the earliest times, strongholds were solely defensives to resist attack by primitive weapons with no great range. The defenders needed an impregnable fortress, in which to shelter. The sophistication grew in response to increased numbers of deliveries from attackers, but the basic balance between attackers and defenders remained until it was upset by Romans' development of 'siege warfare' To counter this came construction of protective shelter inside the besieged area and the erection of tall shelters encircling walls. Thus the balance was maintained and see-saw battle continued until the end of nineteenth century.

The growth in power and sophistication of explosives and fire arms changed the earlier philosophy during World War-I, in

favour of the attacker   The defensive counter-measures merely increased the mass and strength of the structure in response to the more powerful attacks.   The conflict until this time mainly confined to armed forces, who suffered twenty times more causalities than civilians   The next major shift was due to advancement in aerial warfare widely used in World War II   The civil populace behind the front line could for the first time be directly involved in the conflict.   This led to further improvement in defence by development of public and private air raid shelters, which could withstand a local explosion and in some cases, even a direct hit

1.3   Nuclear Environment

The development of nuclear bomb and its first use at Hiroshima (15 kT) and three days later at Nagasaki (20 kT) radically altered the threat posed by the attacker   The amount of nuclear weapon energy is so high that even if military targets are selected, the whimsically named collateral damage would result in an effect little different from that of such purely civilian targets as cities are chosen

Parallel to this, came the remarkable improvement in accuracy of the delivery system of these devastating weapons, which is measured in terms of Circular Error Probabilities (CEPs). In fact some of the latest delivery systems have CEPs even less than a hundred meters.

1.4 Protective Shelters

Thus in society an individual has only opportunity to safeguard an ordered civilization in long term, and that is by pressing the establishment of total disarmament The removal of fear of annihilation so that no nation has enough armament to attack any neighbor nation anywhere, must be the objective. Yet there are many powerful voices around the world, who still believe, 'If you desire peace then be prepared for war' This is dangerous nonsense when the weapons of war are not swords but nuclear warheads and it is a disastrous misconception to believe that by increasing the total uncertainty one increases one's own certainty of survival

Thus the only defence response made possible by these developments is to seek shelter in the immediate area to protect against the harmful effect of the weapons These shelters can broadly be divided into three categories from structural and utility point of view These are

> i)   protective shelters for civilian population.
>
> ii)   upgraded structures for industries
>
> iii)   specialized structures (eg Hospitals, Water supply systems, Government buildings, Command complexes)

As the national security and chances of winning a

nuclear war are completely dependent on the continuity of the chain of the command at the highest level, this present study is focused on planning, design and construction of a Command Complex at the national level to safeguard our military and political leaders in the event of a nuclear war But the parametric studies and analysis of the present work are applicable for any hardened concrete structure to resist the nuclear weapon effects.

1.5   Scope of the Present Study

The scope of the present study is mainly to plan, analyze and design the 'National Command Complex' A hardened concrete structure to mitigate the collateral nuclear weapon effects to the level tolerable to the housed operation/material/personnel is considered. To elaborate more, this protection entails

i)   nuclear blast and shock resistant design,

ii)   protection against radiation for specific period,

iii)   protection against thermal effects, and

iv)   shielding against other effects such as electromagnetic pulse (EMP) ,dust, debris, fires etc.

The aim of the present work is outlined as follows

    i)   Construction of data charts for peak over pressure for various ranges, height of bursts and magnitude of explosion from available analytical expressions

    ii)   Establish pressure time histories for various possible cases of explosions.

    iii)   Threat perception and Reliability analysis for dispersal of facilities.

    iv)   Parametric study to obtain optimal depth of burial for various ranges, height of bursts and magnitude of explosion, taking soil arching effects into consideration

    v)   Radiation analysis for various thickness, grade and type of concrete.

    vi)   Study of attenuation of radiation with depth of burial for optimum depth taking builtup factor into consideration.

    vii)   Thermal Radiation Effect and its parametric study with depth of burial.

    viii)   Static analysis of the principal shell module of concrete for most expected threat by using finite element method.

    ix)   Dynamic analysis (Time History Analysis) of

the modules using Structural Analysis Programm-IV (SAP-IV).

x) Design of the modules by Indian Standard Codes of practice

1 7   General Standard Qualitative Requirements

Some of the suggested qualitative requirements for such a complex are .

i) Capable of housing approximately two hundred persons;

ii) Uninterrupted operation for a minimum of thirty days;

iii) Alternate passages for facilities;

iv) Sufficient dispersal and alternate emergency facilities;

v) Concealed structure;

vi) Emergency entry and exit doors, and

vii) Internal and external communication

1.8   Planning and Layout

Based on the requirements listed in the foregoing and keeping in view the functional aspects, the proposed outline plan of the complex is as shown in Figure (Fig) 1.1. It caters for the

facilities as shown in Table 1 1

Table 1.1   Suggested facilities of National Command Complex

S.No	Name of the facility	Qty
1	Living/Offices Rooms	12
2	Administrative facility	2
3	Power Plant	2
4	Air Filtration Unit	2
5	Hospital	2
6	Cremation Place	1
7	Fire Fighting Unit	1
8	Water Tanks	2
9	Decontamination Stations	2
10	Security Rooms	2
11	Chemical Toilets	6
12	Central Hall	1
13	Communication centers	2
14	Meteorological Station	1
15	Air Suction Unit	2

Apart from these the complex will also have passages to connect all the facilities for the movement of personnel and a jeep size vehicle.

Although the dimensions of these facilities may vary depending upon the actual functional requirements, for the purpose of this thesis, these have been kept at realistical values.

Fig 1.1   Suggested Layout of National Command Complex

Not to Scale

All dimensions are in meters

1.9   Organisation of the Thesis

        The present work has been organised into four chapters
Chapter-I   covers the planning and layout aspect of the complex
keeping in view the qualitative and quantitative requirements.

        In Chapter-II   the available literature on the subject
matter has been reviewed in detail   The aspects such as crater
effects, ground motions and neutron radiation which are not
considered in the present study have also been reviewed for the
sake of completeness.

        Chapter-III   deals with various parameteric studies
performed from optimal dispersal, depth of burial and temperature
considerations   The latter part of the chapter contains analysis
and design of one of the principal modules of the complex   The
results have been discussed at the end of the each section to
facilitate better understanding.

        Chapter-IV   concludes the present work with qualitative
recommendations and future the scope of study for civil engineers
in this challenging field .

CHAPTER - II

REVIEW OF LITERATURE

2.1   Scope

The literature review for the thesis has been classified as follows

i)   Blast and Shock effects of nuclear explosion

ii)   Crater effects.

iii)   Ground motions

iv)   Nuclear radiation effects

v)   Thermal radiation effects

vi)   Other effects (eg EMP,dust, debris and fires)

vii)   Threat perception and reliability analysis for optimal dispersal of facilities.

viii)   Soil arching relations and attenuation of over pressure with depth of burial

ix)   Finite Element modeling for shell structures

x)   Static and Dynamic Analysis

xi)   Design of concrete shell structures

2.2   General

The nuclear weapon effects for protective construction vary with location and the magnitude of explosion. They can be

classified as air, surface or underground burst   This location
based classification is due to the variation in the quantum of the
effects. A burst above 10m height is regarded as an air burst and
the burst taking place below 5m is regarded as an underground
burst [1]   The relative effects due to various burst condition is
shown in Table 2 2.1 [2].   It is evident that the near surface
burst causes maximum damage in terms of blast and radiation   It
is more likely to be resorted by the attacker in the event of
nuclear war. Hence, the analysis and design presented in next few
chapteres caters for this worst possible condition.

Table 2.2.1   Relative Degrees of Weapom Effects for Various
                Burst Conditions [2]

Burst Condition	Thermal Radiation		Initial Nuclear Radiation	Ground Shock	Air Blast	Early Fallout
	Light	Heat				
High Alt.	****	**	*		*	
Air Burst	***	****	****	*	****	
Ground	**	***	***	**	***	****
Water	***	***	***	**	***	****
Confined subsurface				****		

2.3   Blast and Shock Effects

When a nuclear weapon is detonated in the air,
hydrodynamic expansion of bomb debris and radiation heated air
produce a strong shock wave expanding in the surrounding air. Its
interaction with ground surface affects the geometry and

characteristic of this expanding blast wave [1].

A surface or near-surface burst produces a hemispherical shock front that reflects from the ground The reflected signal, travelling faster than the incident shock in the heated air, eventually takes over the incident shock and forms a Mach stem that connects the ground with the triple intersection of incident, reflected and Mach stem shock to form, producing double peak phenomenon. This can be explained as shown in Fig. 2 3.1 The incident wave (1) from a burst point above the ground is reflected in a regular reflection (2) until the angle it makes with the ground plane becomes large enough to allow the reflected wave to takeover and coalesce with the incident wave forming a Mach reflection (3). As the Mach stem grows, the contact surface (4), separating air that has experienced only the Mach shock from air that has been through both the incident and reflected shocks trails behind and connects the triple point (5) with the surface. However, air flow above the contact surface does not completely turn parallel to the surface by the reflected shock and retains some downward momentum This results in eventual compression at the surface (6) as the downward moving double shocked air above the contact surface is stopped This compression (7) distorts and chews up the tail of the contact surface stream line (6) and rises the pressure. The Mach shock itself represents a lower pressure than that behind the reflected wave in the regular reflection region, but the second shock quickly builds to appreciably higher values at the transition. The important aspects of this phenomenon as shown in Fig.2 3.2 (a) and (b) are as follows [1]

Fig   2.3.1   Mechanism of Shock Wave for Near Surface Burst

Fig   2.3.2 (a)   Variation of Over Pressure with

Time at a given location

Fig   2.3.2 (b)   Variation of Over Pressure with

distance at a given location

i)   Time of arrival

ii)   Peak pressure

iii)   Positive phase duration

iv)   Pressure - Time History

2.3 1   Over Pressure and Dynamic Pressure

The transient pressure which is greater than the atmospheric pressure is defined as the over pressure. The peak over pressure is the maximum value of the over pressure at a given location. As the blast wave arrives at a given point, the over pressure rapidly increases from zero to the peak pressure. The magnitude of this peak over pressure and its variation depends on the location and the magnitude of the explosion.

As the blast wave moves outward from the explosion, the flow of the mass of air behind the blast front produces a wind The resulting pressure is termed as dynamic pressure which is a function of density of air and the wind velocity behind the shock front The speed of the shock front U, is given by [1,3 and 4]

$$ U = C_o \left[1 + \frac{6\ P_s}{7\ P_o} \right] \qquad (2.3.1\ 1) $$

where,

Assuming that air is an ideal gas

γ =   Specific heat ratio = 1 4

C_o =   Ambient sound speed

P_o =   Ambient pressure

P_s = Peak over pressure

This approximation is correct within $\pm$ 8 % for the peak over pressure less than 700 MPa [1]

A finite time is elapsed between the detonation and the arrival of the blast front at a given location This time of arrival is dependent primarily upon the weapon yield and distance from the point of burst.

The duration of the blast wave is characterized by two distinct phases, viz positive and negative phases. During the positive phase the over pressure rises very rapidly from ambient to peak value and then subsides more slowly to ambient pressure once again. For some height of burst in the mach reflection region, a second peak pressure increase may occur, which may be higher or lower than the first pulse As the distance from the explosion increases the positive phase of the dynamic pressure becomes some what longer than that of peak over pressure. In the second phase a partial vacuum is created, then the wind blows towards the point of detonation. This phase is comparatively longer than positive phase and the peak rarely exceeds 28 kPa.below the ambient value . Although smaller in magnitude it is important for design of blast doors and latches [1].

Yield Scaling

The air blast parameters are normally given in terms of 1 kt or 1 Mt. These parameters can be determined for other

yields of interest by scaling from the reference values [1]

These scaling laws [1] are

$$\frac{R}{R_1} = \left(\frac{W}{W_1}\right)^{1/3}$$

$$\frac{t}{t_1} = \left(\frac{W}{W_1}\right)^{1/3} \qquad \qquad . \quad . \quad (2.3 \ 1 \ 2)$$

$$\frac{I}{I_1} = \left(\frac{W}{W_1}\right)^{1/3}$$

where

R_1 Range at which pressure of interest occurs

W_1 Reference yield

R Actual range

W Actual yield

t_1 Reference time

t Actual timeand

I_1 Reference impulse

2.3.2   Pressure - Time Histories

Analytical expressions and several graphical methods are available [1 ,2 and 3] to find the over pressures and the time histories. These were developed and used since 1962 after the Nevada test sites results But the detailed experiments conducted in 1970's have provided a better definition of the region of the double peaks, an important area in the early mach reflection region at high over pressures. These highly nonlinear analytical expressions to calculate the peak over pressures and corresponding

time history are given in Apendices 'A' and 'B' These expressions use the scaled ground range and height of burst and thus yield results corresponding to one kT Hence the different times and ranges must be scaled to the actual yield of requirements

2.3.3 Approximate Analysis for Time Histories

If computers are not available to solve these expressions then the time histories can be approximated by triangular equivalents, having the same initial peak-over pressures but different time depending upon the expected time of structural response. These equivalent triangular pulses are as shown in Fig 2 3 3.1 The durations are determined from the Fig 2.3.3 2 . Reference [1] provides the procedural details for approximate analysis

2.3.4 Dynamic Pressure

In many a case the, drag forces associated with the strong transient wind behind the shock front are mainly responsible for actual damage, specially in the case of above ground structures. Some of the structures are described as drag sensitive, as they are quickly enveloped by the blast wave and thus the primary translatory forces are due to the results of the drag forces. These forces are the function of the size, shape and

Fig   2.3.3.1   Equivalent Triangular Pulse

Fig   2.3.3.2   Duration of Effective Triangular Pulse

transient dynamic pressure

The analytical expressions for peak dynamic pressure dynamic pressure time histories, time of arrival, duration and impulse are given in References [1 and 3]. As it is always advantageous to bury the structure for many obvious reasons hence the dynamic pressure is not of much importance in the present context However, this aspect is very important for the above ground structures and should be taken care while designing such structures The references [1,2] give details of this aspect for the design of nuclear structures

2.4 Crater Effects Due to Nuclear Blast

This phenomenon occurs when there is very near, surface or under ground burst The approximate dimensions and other terminology associated with this aspect are as shown in Fig 2.4.1

The dimensions are predicted from two tests conducted at Nevada test site, before nuclear test ban treaty, one in alluvial soil and other in hard rock. For other conditions these can be interpolated The scaling laws exist here to standardize for 1 kT explosion For the other yields crater dimensions can be predicted by applying a yield scaling exponent.

The height of burst (HOB) or depth of burst (DOB) is measured from the original ground surface to the centre of weapon release. The most significant to catering is the low air burst, when HOB less than 3 $m/kT^{1/3}$.

The volume of crater from air burst in various

homogeneous geologies are given in literature [1] and can be estimated approximately

2.5 Ground Motions

Another important phenomenon occuring due to blast in very near surface burst or ground burst is the induced ground motion as shown in Fig 2 5.1 Here the air blast loading is shown in super seismic condition i.e. the velocity of the air blast shock is greater than the propagation velocity of the peak compressive stress in upper material. The initial ground shock is a response to the air blast loading immediately above the point of interest. The ground shock component associated with the local air blast is said to be air slap induced.

As the air blast shock front slows, the velocity becomes less than the propagation velocity of the peak compressive stress in the upper material The initial ground shock response at this time is caused by the air blast upstream from the point of interest Situations where the ground motions are outrunning the blast are of importance from the analysis considerations [1].

The ground shock is divided in two components, the air slap induced and upstream induced components. The wave forms for each are superimposed temporally to arrive at the composite wave form. The ground shock from all sources other than local air blast is considered upstream ground induced shock, including shock from directly coupled energy and upstream air blast. This is further divided into *body wave* and *surface wave components*, because at

LEGEND:

D_a = Apparent crater depth

H_{a_l} = Height of apparent lip

R_a = Apparent crater radius

R_{a_l} = Crater radius to apparent lip

R_e = Ejecta radius

SGZ = Surface ground zero

Fig 2.4.1   Crater Effect

Fig 2.5.1   Ground Shock Phenomenology

longer range the upstream induced motions are primarily associated with surface wave [1]

To gain maximum advantage from the nuclear explosion on the strategical targets, the weapon is detonated in the air. Hence it very unlikely to expect any surface burst from the attacker Therefore this effect has not been considered for the design and analysis in the present context

2 6   Radiation Effects

One of the special features of the nuclear explosion is that it is associated by emissions of the nuclear radiations, which is one of the governing criteria for design of such important structures [5] These radiations can be categorized as

i) α particles

ii) β particles

iii) γ radiation

iv)   Neutron radiations

2.6.1 α and β Radiations

The ranges and penetration power of these two radiations are very limited they cannot reach the surface of the earth from air burst even when the fireball touches the ground Hence the initial radiation consists of mainly γ rays and neutron radiation within a minute of the explosion [2].

Both of these radiations produce harmful effects on living organism as shown in Appendix (Apex) 'C' It is this highly injurious nature of these radiations combined with their long ranges that make them such a significant aspect of nuclear radiation. The energy associated with this is approximately three percent of the total energy release [1]

2.6.2 γ - Rays

As it is evident that the γ rays being the most important aspect of the nuclear radiation as for as the shielding is concerned This is has been reviewed in greater detail under the following parameters.

a) Sources

In nuclear explosion the γ rays are generated due to the fission process. They are also generated by the neutron produced in the fission process. When these neutrons are captured by non fissionable nuclei material they get converted into compound nucleus which is of very high energy state. The excessive energy may be liberated as γ radiation called captured γ radiation. Here the interaction of neutron with nitrogen nuclei is of importance because γ rays produced thereby is of very high energy and attenuates very little with distance. The γ rays are also produced due to inelastic scattering As the fission fragments are highly radioactive in nature they also generate an appreciable

amount of the radiation in the very first minute of the explosion

This radiation is known as *delayed gamma radiation* [2]

b)   Technical   Aspect of γ radiation

Rigorous analysis of the radiation calculation due to γ rays needs the knowledge of interaction of the γ rays with matter, as a result of which photons are scattered or absorbed   These interactions can be classified as follows [5]

i)   Compton effect

ii)   Photoelectric effect

iii)   Pair Production

Compton   effect

The *total extent of compton scattering per atom of* material with which the radiation interacts is proportional to the number of electron in the atom i.e to the atomic number for all materials, irrespective of their atomic weight.   The effect is shown in Fig 2.6 2 1.(a) [5].

Photoelectric effect

It is an interactive process in which an orbital electron is ejected from an atom by a photon.   This occurs when photon possesses a higher energy than binding energy of the

orbital electron with which it collides   All the energy of the
incident photon in excess of the electron binding energy is
transformed into kinetic energy of the ejected photo- electron
As the binding energy of the orbital electron increases the
photoelectric effects decrease rapidly as inversely proportional
to the cube of energy.   The photoelectric effect is proportional
to the fifth power of the atomic number and the microscopic
cross section is proportional to (N $Z^5 E^3$ ^{5})   The other forms of
radiation may also arise but they can be disregarded for practical
purposes   The phenomenology is sketched as shown in Fig
2.6.2 1 (b) [5].

Pair Production

The process in which a photon is converted into a pair
of electron, positron and negatron, in the coulomb field of an
atomic nucleus is called pair production   The incident photon is
replaced by a positron-negatron pair   All the energy is absorbed
As the rest mass of an electron is equivlant to 0.51 Mev. Thus to
have the kind of pair production incident photon should not have
energy less then 1 02 Mev.   The balance of the photon energy then
appears as kinetic energy (KE) of the electron-positron pair.

The probability of pair production is more when the
atomic number Z of the absorber is high.   The cross section can be
approximated to Z^2.   The cross section also increases with the
photon energy, and at high energies it becomes the dominant
interaction process of photons with matter (Fig.2.6.2 1 (c)).

Incident photon (E_0)

Orbital electron

Scattered photon (E')

Recoil electron

E = energy

(a)   Compton Scattering

Incident photon

Photoelectron

O Orbital electron
● Photoelectron
O Neutron
● Proton

(b)   Photoelectric Effect

Nucleus

Incident photon
$E > 1.02$ MeV

e⁻

e⁺

e⁻ Negatron
e⁺ Positron

(c)   Pair Production

Fig   2.6.2.1.

Hence it can be concluded that interaction of photon increases with the increase of atomic number of the material through which the γ ray passes. Each interaction does completely absorbs or reduces the energy of incident photon Hence it can be said that material containing the elements of high atomic weight will be more effective as γ ray shield Also with energy greater than 1 02 Mev the absorption is minimum. This process of the interaction is shown in Fig 2 6.2 1 (c) [5 and 6]

c)   Photon Attenuation

Consider a slab of absorber material placed between a narrow collimated source of mono magnetic photons and a narrow collimated detector as shown in Fig 2.6 2.2. The arrangements are such that the scattered radiation from striking the detector and any interaction of photons with the absorber material are prevented leading to complete removal of photon from the beam.

Then, in a thickness dx of the absorber the fractional reduction in the photon intensity I is given as $-dI/I$, which is related to the narrow beam attenuation μ and the thickness dx by the following relation

$$dI/I = \mu dx \qquad\qquad\qquad (2.6\ 2.1)$$

If the initial photon intensity is I_o and the thickness of the absorber is x then

$$\int_{I_o}^{I_x} \frac{-dI}{I} = \mu \int dx \qquad\qquad (2\ 6\ 2\ 2)$$

and

$$I = I_o\ e^{-\mu x} \qquad\qquad (2\ 6\ 2.3)$$

These equations are referred as exponential absorption equations

The linear absorption coefficients are dependent on the density of the material   The density often does not have a unique value but is dependent on the physical state of the material   Thus to obviate the effects of variations the linear absorption   coefficient for reference purposes is expressed as mass attenuation coefficient (μ/ρ) [5 and 6].

d)   Photon Absorption

The energy absorption coefficient are related with the loss or absorption of energy as a result of photon interaction with matter, whereas the attenuation coefficients concern the number of photons which are affected. Thus the amount of energy absorbed determines the effect of radiation   Similar to the attenuation coefficients the values of the absorption coefficients are available in references [7]

e)   Broad Beam Attenuation and Buildup Factors

The above mentioned equations are only applicable to cases in which the scattered compton interaction may be regarded as essentially removed from the γ ray beam. It reasonably holds good for narrow beams or for the shields of narrow thicknesses but fails for broad beams or thick shields, which is the case in nuclear explosion The allowance of multiple scattering is made by the provision of a 'buildup factor as shown in Fig 2 6.2.3. Hence these equations can be modified as [5]

$$I = I_o B(x) \ e^{-\mu x} \qquad\qquad (2\ 6\ 2.4)$$

where

    $B(x)$ Buildup factor

The buildup factor depends on many factors such as energy of the photon source, angle of incidence, nature, thickness of the shield and the type of detector response   The values of the buildup factors for various ranges of energy and shield material is given in references [7].   However, some of the relevant ones for the purposes for the thesis are given in Apex 'D'

f)   Transmission of γ ray and Source Geometry

A point source is regarded as a volume of the source material the dimensions of which are small in comparison with the distance between the source and the position of the detector   If a point source emits particles in all the directions isotropically, the radiation is assumed to be evenly distributed

Fig 2.6.2.2   Narrow Beam Attenuation

Fig 2.6.2.3   Broad Beam Attenuation

over the surface of a sphere whose area is $4\pi x^2$, where x is the distance between the source and detector   The flux at a distance x is given by [2 and 5]

$$\phi = \frac{S_o}{4\pi x^2} \qquad\qquad (2\ 6\ 2.5)$$

where

ϕ =   The particle flux

S_o =   Strength of the source

If it is considered that the point source is surrounded by a spherical shield then the flux density at a distance x from the source is

$$\phi = \frac{S_o}{4\pi x^2}\ e^{-\mu t} \qquad\qquad (2.6\ 2\ 6)$$

where

t Thickness of the shield

g) γ Ray Spectrum

The information concerning the energy spectrum of the initial radiation is important because of the susceptibility of the living organism under various energy spectra. The attenuation properties of the air, shielding material and the response of the

detector instrument is dependent on the energy distribution of the γ-rays   Although the exact spectrum at some distance from the source is difficult to obtain but with the knowledge of initial γ radiation spectrum at the source and existing data on scattering and absorption of different energy in the intervening medium can be employed to provide the spectrum at a given distance Reference [2] provides relevant information on this important aspect of the nuclear explosion.

2.6.3   Neutron Radiation

As in the case of the photons, which interacts with the electrons in atoms, the interaction of the neutrons with electrons is negligible. They interact rather with the nuclei of the atoms, and their interaction is very much dependent on the KE of the neutrons.

a)   Nuclear Reactions

Nuclear reaction generally be expressed by the following type of the equations [5]

$$a + X \longrightarrow b + Y \qquad\qquad (2.6.3.1)$$

where

X Target nucleus

Y Resulting nucleus

a   The bombarding particle

b   Emitted particle

In the transmission of the neutron through matter many types of reactions or interactions are possible   In the shielding calculations for neutrons the reaction which are significant are [3] elastic, inelastic and neutron capture.

b)   Effective Removal Cross Section

Most neutrons which penetrate thick shields are fast neutrons, having energy greater than 7 Mev. The effective removal cross sections are the cross sections which may be used in exponential absorption equation to obtain valid results concerning the attenuation of fast neutrons [5]   Hence,

$$I = I_o \, e^{-\sum R_x}$$

(2.6.3.2)

Where

$\sum R_x$ Effective   macroscopic   removal   cross section for material

I_o Initial fast neutron intensity

I Emergent fast neutron intensity

But, if the sufficient number of hydrogen atoms are not in the shield then the intensity of the emergent neutron may be higher than the calculated from equation 2.6 3 2 [5]

Similar to the photons the energy spectrum for the neutrons from explosion of nuclear bombs are available in the literatures [2] The calculation for the integrated neutron flux can also be done in similar fashion

For greater effects in terms of radiation special Neutron Bombs are available with most of the developed countries but they do not generate significant amount of shock effects The most part of the energy of these weapons are consumed to liberate radiation particles producing very little shock effects Since, the shock effects are the principal criteria for design of such structures, the effects of neutron radiation due to fission bombs in calculations can be neglected without much loss of accuracy [5]

2.7   Thermal Radiation

Thermal radiation is rarely a driver in the design of a hardened structure. By making provisions for protection against sterner threats of nuclear blast and nuclear radiations the designer almost automatically protects the structure against thermal radiation threat. However, it is pertinent to evaluate the thermal effects to the internal environment of the facilities. Also the study of thermal effects are important for the structural engineer to incorporate the temperature effects in the analysis

and for the selection of appropriate material accordingly. The approximate radiant exposures for ignition of various materials for low air bursts are given in literature [1 and 2].

2.7 1   Technical Aspect of Thermal Radiation

Although spectroscopic studies made in course of weapon tests revealed that it does not behave exactly like a black body, the assumption of a black body behavior for the fireball, however serves as reasonable approximation in interpreting the thermal radiation emission characteristics. For a black body the distribution of radiant energy over the spectrum can be related to the surface temperature by Plank's equation [2 and 8] as

$$E \lambda \;=\; \frac{8\,\pi\,h_c}{\lambda^5} \cdot \frac{1}{e^{h_c \,/\, \lambda kT} - 1} \qquad (2.7.1)$$

where

E	Energy of the black body
c	Velocity of the light
h	Plank quantum action
T	Absolute temperature
hc/λ	The energy of the the photon wavelength.

The rate of emission of energy J_λ can be given for a black body for a given wavelength[2 and 8]

$$J_\lambda = \frac{c}{4} E \qquad\qquad (2.7\ 2)$$

where

J_λ Energy per unit area

According to Stefan Boltzman law the total amount of energy J *radiated* per unit area per second is given by

$$J = \sigma\ T^4 \qquad\qquad (2.7\ 3)$$

where

σ Stefan Boltzman constant

$\quad = \quad 2\ \pi^5 k^4 /\ 15\ h^3\ c^2$

$\quad = \quad 5.67\ E\text{-}5\ erg/cm^2.s$

Next important parameter to be considered is the total thermal energy received at some distance D from the point of explosion which can be given by the law of physics [2] as

$$Q = \frac{E_{tot}}{4\ \pi\ D^2} . e^{-kD} \qquad\qquad (2.7.4)$$

where

k Absorption coefficient of the air

E_{tot} The fraction of the total weapon energy available as effective thermal radiation

Q Total energy received at distance D

It is also important to know the total duration of the effective pulse for the calculation of the incident energy at any distance on the earth surface. Although no theoretical formulas are available for this time pulse time calculation, the tests conducted at the Nevada test site before nuclear test ban treaty provide some guidelines to evaluate this pulse time The graphs are available for various energies of the explosion in literature [2].

The attenuation of the thermal energy by a transient source in any medium is a complex function of the conduction and radiation phenomenon It depends on the thermal properties of that medium and can be evaluated for the buried structure. Reference [9 and 10] provides the fundamental approach in this aspect of thermal radiation.

2.8 Other Effects

The other important effects of nuclear weapons which could be of importance to a design engineer are as follows

i)   Electromagnetic Pulse Effects

ii)   Debris

iii)   Dust and

iv)   Fires

2.8.1   Electromagnetic Pulse Effects

The nuclear explosion releases large amount of energy.
Approximately one percent of it get converted in EMP. The nature
of the pulse depends on the type, magnitude, range and the height
of explosion. Its effect on any system depends on the physical
and mechanical characteristics and the location of the system.
These effects are more relevant to electronic equipments which are
to be housed inside the complex Special care should be taken for
installation of these equipments [1 and 2]

2.8.2   Debris

Debris is any material that can be carried along by the
blast from a nuclear explosion. Such a material can cause
causalities and damage to the facilities as a result of high
energy impact or accumulation, or both This effect may cause
severe damage to above ground and mounded structures. But due to
many obvious reasons these command complexes are either shallow or
deep buried, where the effects of debris are none Hence this
effect has not been discussed in great detail. However,
literature provides adequate information to combat this threat
[1].

2 8.3   Dust

The dust is produced due to the following two reasons

      i)   Propagation of the blast wave from the point of explosion

      ii)   Thermal energy produced due to the blast

This phenomenon is again pertinent to above ground and mounded structures and therefore has not been reviewed keeping in view of the present requirements [1]

2.8.4   Fires

Although shallow buried structures have very little probability of catching fires, But civil engineers should avoid use of fire prone materials in construction of such complexes. References [1 and 2] give details of the threshold energy of various materials of civil engineer's concern [1 and 2].

2.9   Threat Perception and Reliability Analysis

The threat perception and accordingly reliability analysis depends on various strategical and classified military informations   If the information on the attacker's objective and defender's actual requirements are available then this can be performed for actual scenario.   In the present

context, due to absence of the actual information this has been performed only for dispersal of the facilities by assuming fictitious capability of the attacker   However some of the guidelines available in Reference [1] can be summarised are as follows

    i)   Develop demand scenario

    ii)   Identify the failure modes and criteria

    iii)   Calculate demand applied in each mode

    iv)   Construct series and parallel network of failure mode probabilities

    v)   Allocate goal to each failure mode

    vi)   Calculate for each failure mode, capacity required to satisfy allocated share the goal

    vii)   Identify worst case mean capacity for each failure mode and,

    viii) Write, for each failure mode, deterministic design specification for identified   worst case mean capacity

2.10   Blast Loading and Soil Arching Effects

The choice of siting the complex is basically a compromise between the strategical and technical requirements The complex can be above ground, mounded or buried. The type and the quantum of the force subjected on the structure for each of these choices are totally different   Therefore the approach for

analysis is different for each of these choices.   The loading on
the structures for below ground structures have been described in
next few sections

2.10.1   Air Blast Loading on Below Ground Structures

The   below   ground   structures   can   be   categorized   as
shallow or deep buried depending on the depth of the burial (DOB).
This division is relative and depends on the span of the structure
The classification is as given below [1 and 11].

i)   Shallow buried   (0.2L <= DOB <= 1 5 L)

ii)   Deep buried   (DOB > 1 5 L)

where

L   Span of the structure

The   design   of   deep   buried   structures   is   primarily
governed by the soil overburden pressure.   The blast has very
little effect on the structure.   These structures have other
peculiar problem associated with them.   They are generally not
economical and hence not preferred unless warranted.   Therefore as
a   part   of   literature   review   these   structures   have   not   been
considered.

The shallow buried structures experience partially the
blast load due to soil arching and at the same time they are also

influenced by the soil overburden   The total effects are
different at different depths   Hence for ease of the analysis
these can further be classified as [1]

        i)   Shallow Buried

      ii)   Surface Flushand,

    iii)   Mounded Structures

2.10.2   Shallow Buried Structures

The shallow buried structures have a DOB over the roof
or crown, such that $0.2 L \leq DOB \leq 2.0 L$.   where L is the clear
span between the supporting walls of a roof slab or the horizontal
diameter of an arch or cylindrical structure   The structures
located at $0 \leq DOB \leq 0.2 L$ are treated as surface flush   The
loads   produced by the nuclear explosion on the structure buried
in a medium with finite shear strength are influenced not only by
structure/medium interaction as the loaded structure deforms but
also by the effects of propagating transient stress wave [1]   A
typical shallow buried structure is as shown in Fig 2 10.2.1.

2.10.3   Soil Arching

It is defined as the ability of the soil to transfer the
loads from one location to the another in response to a relative
displacement between the locations   Thus it is solely dependent

(a) BURIED HORIZONTAL CYLINDER

(b) VERTICAL STRESS COMPONENTS ON HORIZONTAL CYLINDER
SHORTLY AFTER ARRIVAL OF THE INCIDENT WAVE

Fig 2.10.2.1   Shallow Buried Structure

on the properties of the soil   This can effectively redistribute
the loads on a roof slab away from the flexible center of span to
 hard support points such as columns and structural walls   This
has also been practically verified for buried arch structures The
effect of soil arching is to force a high mode compression
failure.   For very hard structures the soil arch may not form
because the shear capacity of the soil may have exceeded, and no
redistribution   would   have   occurred   Various   analytical
expressions are available to incorporate these effects [1, 12, 13
and 14]   But   the   most   generalized   equation   based   on   a
differential approach that produces realistic results is given in
Reference [1] and rewritten as

$$\frac{P_q}{P_{so}} = \exp\left[\frac{-2K_o(\tan\phi)(a+1)bL^2}{aL^2}\right]$$

..(2.10.3 1)

where

P_q Stress applied at the top of the structure ,

P_{so} Ground surface over pressure

K_o Coefficient of earth pressure at rest

ϕ Angle of internal friction for soil

L   Span length of the structure

a   Factor relating length of a structure to its
       span length

b   Factor relating depth of burial to its
       span length

       Fig 2.10 3.1 shows soil arching as a function of depth
of burial.

(a) BURIED RECTANGULAR STRUCTURE   (b) BURIED ARCH OR CYLINDER

Fig   2.10.3.1   Soil Arching as a Function of Depth of Burial

2.10.4   Shallow Buried Rectangular Structures

Predicting loads on structures is further complicated by the fact that stress wave propagating downward reflects at the structure surfaces which are in the path of propagation.   This reflected wave is released by one of the three mechanisms   When the structure begins to move as a rigid body with free field, by a rarefaction wave travelling inward from the lower stressed field surrounding the buried structure or by tensile wave reflecting back from the concrete–air interface at the bottom of the roof [1].   At very shallow depths it is very likely that a relief wave will be reflected back from the ground surface   Assuming that the reflected stress is relieved first by reflections from the concrete – air interface at the bottom of the roof the approximation for analysis can be done as follows [1]

$$\sigma r(t) = \sigma ff(t)\left(2-t/t_d\right) \qquad for\ t<=\ t_d$$

$$\sigma r(t) = \sigma ff(t) \qquad for\ t>\ t_d$$

where   (2.10.4.1)

$\sigma r(t)$ The stress acting at the roof at any

time t

$\sigma ff(t)$ The incident stress wave

t_d $=$ 12 D/C

C   Compression wave velocity

D   Thickness of the roof surface

The time t can be taken as zero at the time incident wave strikes the roof surface   Also for high yield weapons it is reasonable to assume the incident pressure as ground surface pressure but for low yield weapons less than 50kT it is recommended to take soil arching into consideration.   Thus the equations can be rewritten as

$$\sigma_r(t) = \sigma_{ff}(t)\left[\,2-t/t_d\,\right] \quad \text{for } t <= t_d$$

$$\sigma_r(t) = C_a\ \sigma_{ff}(t) \qquad \text{for } t > t_d$$

(2.10 4.2)

where

    C_a Soil arching ratio

The stress acting at the base of the structure is given by

$$\sigma_b(t) = \rho\ C_L\ v(t) \quad ..(2\ 10.4\ 3)$$

where

    ρ Density of the soil

    C_L Compression wave velocity of the soil

    $v(t)$ Velocity of the structure.

An acceptable approximation to the stresses acting at the base can be given by

$$\sigma_b \ (t) = \sigma\!f\!f \ (t) \qquad\qquad (2\ 10\ 4\ 4)$$

The stresses acting at the side of the structure can be given by

$$\sigma_s \ (t) = K_o \ \sigma\!f\!f \ (t) \qquad\qquad (2\ 10.4.5)$$

where

K_o Coefficient of the lateral earth pressure at rest

2.10.5   Shallow Buried Shells

The analysis of a shell structure is complicated by its geometry [1,15]. The multidirectional effects become important at the instant the incident wave strikes the structure. The process of the interaction can be described as shown in the Figs 2 10.5.1 (a) and (b).

As the incident wave strikes the upper crown of the structure, the stress at the crown is assumed to be double and due to this, structure begins to moving down as a rigid body. Within a very short period of time the entire half portion of the shell experiences stresses due to motion of the cylinder into the soil, while the incident wave has not progressed far beyond the crown As the incident wave propagates downwards, reflected wave continues to occur on the upper half of the cylinder because the peak reflected stress is a function of the angle between the

(a)   DOB Less than 0.2 L

(b)   DOB greater than 0.2 L

Fig 2.10.5.1   Interface Stress on Roof

incident wave and tangent to the cylinder at the point where the incident wave contacts the cylinder, as well as function of the velocity of the structure at the time the incident wave arrives at the point   The load modeling on the structure is shown in Fig 2 10 5 2 [1].

By idealizing the cylindrical structure as octagon the load in the vertical region A can be given by

$$F_a(t) = 0.8 \ \sigma_a \ (t) \ R \ L \qquad (2 \ 10.5.1)$$

where

$F_a(t)$ Total vertical load in the Region A

R   Cylinder outside radius

σ_a Stress in the region A

The load in the region B can be given by

$$F_b(t) = 0 \qquad\qquad For \ \ 0 <= t < 0 \ 3 \ R \ / \ CL$$

$$F_b(t) = 1 \ 2 \ \sigma_b \ (t) \ R \ L \quad For \ \ t >= 0.3 \ R \ /C_L$$

$$.. \ ..(2.10 \ 5.2)$$

The total resisting incident load is taken as

$$F_r(t) = 2 \ \rho \ C_L \ v(t) \ R \ L \qquad\qquad . \ ...(2.10.5.3)$$

(a) OCTAGONAL APPROXIMATION AND ACTING LOADS

(b) AVERAGE VERTICAL STRESS
IN REGION A

(c) AVERAGE VERTICAL STRESS
IN REGION B

Fig 2.10.5.2   Approximate Vertical Loads for Estimating Vertical Rigid Body Motion of a Typical Shell

Hence ignoring shear the equation of motion can be given as [1]

$$M \, v(t) \;=\; F_a(t) \;+\; F_b(t) \;-\; F_r(t) \qquad (2.10\ 5.4)$$

where

$\dot{v}(t)$ Accelaration of the structure

M   Mass of the structure

Another simplified method to analyze these buried shell structures by approxmating the blast force and lateral pressures is shown in Fig 2.10.5.3 [1], is suitable for use with single degree of freedom system analysis which gives reasonable results.

2 10.6   Mounded Structures

The loads expected on these structures are intermediate between the above and underground cases. The inclined earth boundaries reduce the drag and reflected pressure to quite an extent but even then it is very significant up to a slope of 1:4 The geometric complexity and non-uniform loading associated with mounded structures are not readily translatable into simple interaction model. However the bounding loads and motions of the mounded structures can be estimated by considering the above ground, buried or surface flush extreme. Since there are other

(a) ARCH

(b) CYLINDER

Fig 2.10.5.3   Simplified   loading   of   Buried   Arches   and
Cylinders

effects of explosion which are more dominant on these structures, this choice is not suitable for the complex.

2.10.7   Surface Flush Structures

When the DOB is less than 0 2 L   the   structure is treated as surface flush due to its different response than shallow buried structures   The load acting on the roof of the structure can be analyzed as follows   [1]

$$\sigma_r(t) = \sigma ff(t) \left(2 - t / t_d' \right) \qquad \text{For } t <= t_d'$$

$$\sigma_r(t) = \sigma ff(t) \qquad\qquad\qquad \text{For } t > t_d'$$

$$.(2.10\ 7.1)$$

where

$\sigma_r(t)$ Stress acting on the roof at any time t

t_d' Z_s / C_L or 12 D/ C whichever is smaller

Z_s Depth of the structure roof <= 0 2L

As far as pressures at side and base of the structures are concerned they can be taken same as in case of the shallow buried ones.

2 11   Analysis and Design

The analysis of shell structures can be performed either as thin or thick shells [16 and 17]   The thin shell analysis does not take into account the stresses and moments in the direction along the thickness of the shell assuming it to be of a very small quantity   The thin shell analysis approach can be adopted in the present context without much loss of accuracy in the results As the structure and loading are symmetric about one axis

The   membrane stresses and bending moments can be calculated by the following general shell equations [17]

$$T\text{x}   = \frac{\partial^2 F}{\partial Y^2} \qquad\qquad\qquad (2.11\ 1)$$

$$T\text{y}   = \frac{\partial^2 F}{2} \qquad\qquad\qquad (2\ 11\ 2)$$

$$T\text{xy}   = \frac{\partial^2 F}{\partial X \partial Y} \qquad\qquad\qquad (2.11\ 3)$$

$$M\text{x} = D\left(\frac{\partial^2 w}{2} + \nu\frac{\partial^2 w}{2} \right) \qquad\qquad (2.11.4)$$

$$M\text{y} = D\left(\nu\frac{\partial^2 w}{\partial X^2} + \frac{\partial^2 w}{\partial Y^2} \right) \qquad\qquad (2\ 11\ 5)$$

$$M\text{xy} = -D\left(1 - \nu \right) \frac{\partial^2 w}{\partial x \partial y} \qquad\qquad (2\ 11\ 6)$$

where

F Stress   function   which   gives   the   in   plane

stress when the bending is also considered

w   Deflection along z- axis

D Flexural rigidity $\quad = \dfrac{E\ d^2}{1\ -\nu^2}\quad$ and

ν Poisson's ratio

The analysis of the shells can be performed using SAP-IV [18]. This current version of SAP-IV has facilities for static and dynamic analysis of linear structural systems. This program has proven to be a very flexible and efficient tool. This is coded in FORTRAN-IV and can easily be modified as per the requirements. The fundamental approach for static and dynamic analysis using SAP-IV are given in next sections

2.11.1 Static Analysis

The static analysis performed by the SAP-IV can be summerised as follows

i)   A static analysis involves the solution of the equilibrium equations [18]

$$K\ u\ = R \qquad\qquad\qquad (2.11\ 1\ 1)$$

which is followed by the calculation of element stresses

ii)   The load vector R is assembled at the same

time as the structure stiffness matrix are formed. The solution of the equation is obtained by the large capacity linear equation solver SESOL This subroutine uses the Gauss elimination on the positive definite symmetrical system of equations In the program, the $L^T DL$ decomposition of K is used and hence

$$L^T v = R \qquad (2\ 11\ 1\ 2)$$

$$v = D\ L\ u \qquad (2\ 11\ 1\ 3)$$

where the solution for v in the equation is obtained by the reduction of the load vectors,the displacement vectors u are then calculated by back substitution [18].

iii) After the nodal point displacement has been evaluated, sequentially the element stress displacement matrices are read and the element stresses are calculated.

2.11.2 Dynamic Analysis

The dynamic analysis is performed to obtain the following parameters

-Free vibration frequencies

-Mode shapes

-Displacements and rotations

-Stress and bending moments

The approach of the SAP-IV for the analysis is as described in the following

i)   The mode shapes and frequencies are obtained by solution of the generalized eigenvalue problem [18]

$$K \phi = \omega^2 M$$ (2 11 2 1)

where

   ω Free vibration frequency

   ϕ Mode shapes

ii)   In the dynamic response analysis the solution of the equation of the equation [18]

$$M \ddot{u} + C \dot{u} + K u = R(t)$$ (2 11.2 2)

where

   R(t)   Can be a vector, arbitrary time varying or effective loads resulting from ground motion.

iii)   In the present context of the thesis R(t) is
an arbitrary time varying load due to a nuclear blast at
a given range and depth of burial   Hence the Response
History Analysis by direct integration is performed using
SAP IV

iv)   The program uses Wilson-θ method, which is
unconditionally stable.

v)   The Rayleigh damping is assumed, which can
easily be taken into account in the form of mass and
stiffness proportion and is given by the equation

$$C = \alpha \, M + \beta \, K \qquad\qquad (2\ 10\ 2.3)$$

where

α and β are mass and stiffness proportional damping
coefficients.

2.11.3   Design

The design of structure is performed by using
following Indian Standard Codes of Practices

IS:456(1978)   Plain and Reinforced Concrete[19]

IS·2210(1962)   Shell and Folded Plates[20]

IS:4991(1968)   Blast Resistant Design[21]

The check on the limiting stress is given in [22] for plates and shell elements

2.12   Comments on Literature Review

It is evident from the foregoing review that the literature provides sufficient guidelines and approach for designing these structures   The approach may vary depending upon the requirements of the defender   The following points are considered for design of complex

ı)   It has been experienced that the above ground structures are economical only for peak over pressures less then 170 kPa.   But for below ground structures the depth of the burial is a factor which depends on various economical and structural load parameters, which is one of the findings of the thesis

ii)   The choice of below ground structure is due to the following reasons

- It fulfills the military requirements

- It does not experience dynamic pressure which is generated due to the following wind.

- The radiation is taken care by the soil thickness which is an economical and

effective radiation shield material.

- Thermal radiation does not have significant effects on the below ground structures.

iii)   Although the choice of burial reduces the impact of the nuclear forces but it presents a complicated loading due to the following

- Structures experience static soil overburden pressure in addition to the blast pressure
- The load prediction on these structures is complicated due to the soil arching effect
- The transient stress wave propagation in the medium with finite shear strength is a complex phenomenon
- The structure is subjected to active or passive earth pressure

iv)   The shells are preferred because of their shape which makes the magnitude of the net loading smaller than that developed on the box shaped ones.   In addition they (domes and arches) have a great vertical and lateral strength characteristics and may be of the most economical form .However added cost is needed in terms of forms.

v)   The cylindrical and spherical shells and their

combinations are a better choice, as the loading is symmetric. These can be analyzed as thin shells using standard methods for membrane and bending components

vi)   The finite element modeling of the modules can be done by assuming the modules on the rigid foundation. The other nodes have degrees of freedom in all the six directions The loading may be either static peak over pressure or the time histories depending upon the choice of the analysis The openings can be modeled by assuming different element type and material properties at those positions

vii)   The thin shell analysis is performed since the shells do not have significant displacements and rotations in the direction of the thickness

viii)   The membrane stresses and bending moments can be obtained using SAP-IV [18] with suitable modifications.

ix)   The design of the shell structures should be performed by using IS-456(1978) by limit state method for the principal modules of the complex

x)   The check for critical stress due to buckling should be performed as per IS-2210(1962) code for shell

structures

xi) The Johnasen's failure theory for concrete shells/plates has been applied in the present context for checking principal moments in the structures The Reference [22] provides adequate details on this aspect

CHAPTER - III

DESIGN AND ANALYSIS

3.1   Proposed Algorithm

Taking into consideration the available technical information on the subject matter and the defence strategical requirements, an algorithm shown in Fig 3 1 1 is suggested, to design a specialized structure as command complex, subjected to multifacet forces This suggested algorithm incorporates the various possible effects of nuclear explosions at appropriate stages   Thus a basic guideline to design such complexes of national interest is suggested.

The planning and layout of the complex in the foregoing has been done as per this algorithm.

3.2   Parametric Studies

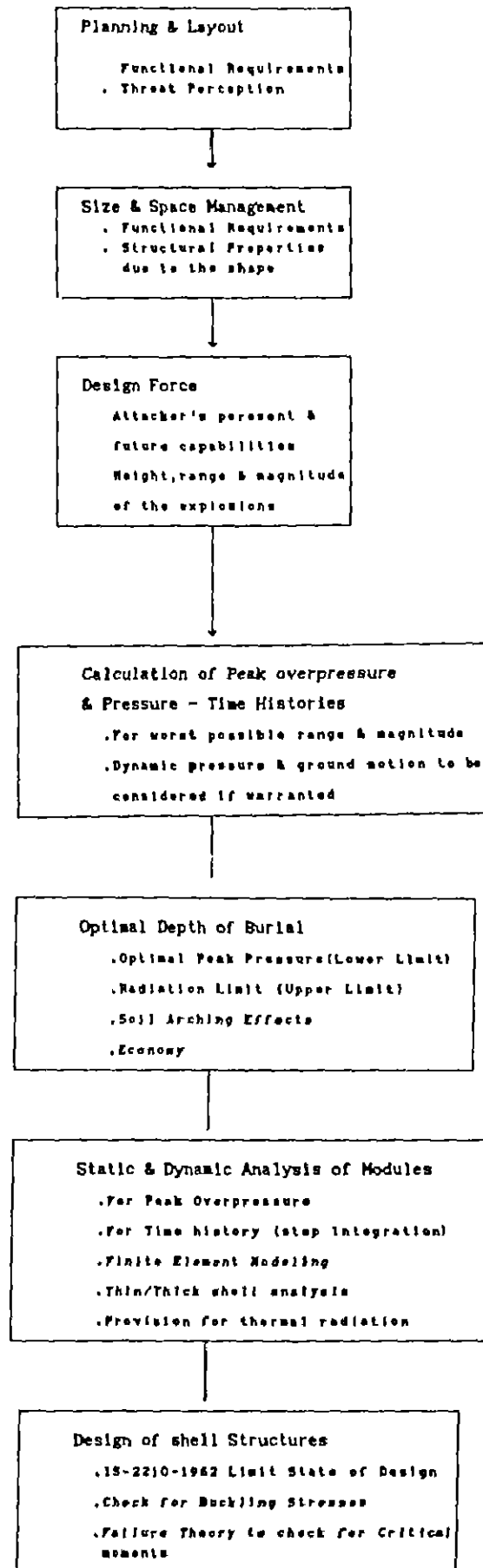Various parametric studies which are general in nature for any type of the nuclear blast resistant structures may be carried out using the foregoing algorithm stated in Fig 3.1 1.

3.2.1   Dispersal Analysis

This analysis has been performed to obtain the optimal dimensions and maximum dispersal of the complex keeping in view the attcker's capabilities. The assumptions made to perform this

```
┌────────────────────────────────┐
│  Planning & Layout             │
│                                │
│       Functional Requirements  │
│     . Threat Perception        │
│                                │
└────────────────────────────────┘
                │
                ▼
┌────────────────────────────────┐
│  Size & Space Management        │
│      . Functional Requirements  │
│      . Structural Properties    │
│        due to the shape         │
└────────────────────────────────┘
                │
                ▼
┌────────────────────────────────┐
│  Design Force                   │
│      Attacker's persent &       │
│      future capabilities        │
│      Height,range & magnitude   │
│      of the explosions          │
└────────────────────────────────┘
                │
                ▼
┌────────────────────────────────────┐
│   Calculation of Peak overpressure  │
│   & Pressure - Time Histories       │
│      .For worst possible range & magnitude │
│      .Dynamic pressure & ground motion to be │
│       considered if warranted       │
└────────────────────────────────────┘
                │
                │
┌────────────────────────────────────┐
│   Optimal Depth of Burial           │
│        .Optimal Peak Pressure(Lower Limit) │
│        .Radiation Limit (Upper Limit)  │
│        .Soil Arching Effects        │
│        .Economy                     │
└────────────────────────────────────┘
                │
                │
┌────────────────────────────────────┐
│   Static & Dynamic Analysis of Modules │
│        .For Peak Overpressure       │
│        .For Time history (step Integration) │
│        .Finite Element Modeling     │
│        .Thin/Thick shell analysis   │
│        .Provision for thermal radiation │
└────────────────────────────────────┘
                │
                │
┌────────────────────────────────────┐
│   Design of shell Structures        │
│        .IS-2210-1962 Limit State of Design │
│        .Check for Buckling Stresses │
│        .Failure Theory to check for Critical │
│         moments                     │
└────────────────────────────────────┘
```

analysis are given in succeeding paragraph

Assumptions

Assuming that the attacker has capabilities to

    i)   launch only one bomb at the complex

    ii)   obtain the correct location if the target size = A_{cl}

    iii)   correctly aim at the target if the target size = A_{cl}

Based on the above mentioned assumptions the problem is formulated as given below

Formulation for Dispersal Analysis

If

    the max plan area of the facility = A_f and,

    the area of the complex   = A_{sc}

then,

the probability of obtaining correct location for a target size A_f

$$pocl(A_f) = A_f / A_{cl} \quad \text{if } A_f < A_{cl}$$
$$= 1 \quad \text{if } A_f >= A_{cl}. \quad ..(3\ 2.1\ 1)$$

probability of correctly aiming at the target size A_f

$$pca(A_f) = A_f / A_{ci} \quad \text{if } A_f < A_{ci}$$
$$= 1 \quad \text{if } A_f >= A_{ci} \quad (3\ 2\ 1\ 2)$$

Probability of correctly aiming the target once located

$$pcal(A_f) = poci(A_f) * pca(A_f). \quad .. \quad . \quad (3\ 2\ 1\ 3)$$

Also,if

CEP_r Circular probable error of the warhead

delivery with respect to known aim point

CEP_e Circular probable error in locating the

attacker's aim point

then

the expected value of the warhead - strike distance R

is (Fig 3 2.1 1) given by [1]

$$R = 1.064\ sqrt(CEP_r{}^2 + CEP_e{}^2) \quad . \quad (3\ 2\ 1\ 4)$$

and if the probability of the warhead landing in the

radius L_r

$$p(wl) = L_r{}^2/ R^2 \quad \text{if } L_r < R$$
$$p(wl) = 1 \quad \text{if } L_r >= R \quad .. \quad (3\ 2.1.5)$$

where

L_r is the radius defined by the attacker for

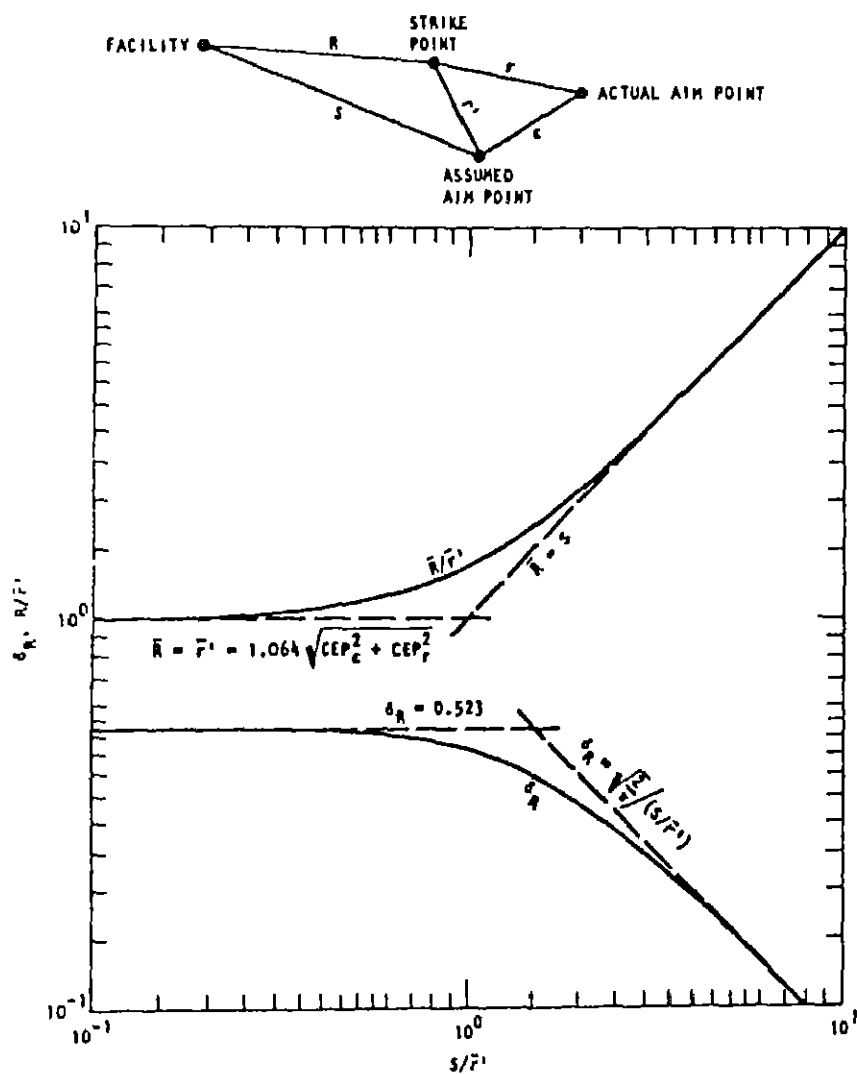its successful mission

Fig   3.2.1.1   Expected   Value   (R)   and   Coefficient   of
                   Variation (dR) of Weapon Strike Distance for
                   Nearby Aim point

If, the probability of the explosion is p(e), then the probability of a successful mission

$$ps(A_f) = pcal(A_f) \quad p(wl).\frac{N}{2} \quad p(e) \quad (3\ 2\ 1\ 6)$$

where

N	number of delivery
p(e)	probability of the explosion of the warhead once launched

and the probability of failure of the attacker's mission can be given as

$$pf(A_f) = 1 - ps(A_f). \quad \ldots \quad . \quad (3\ 2.1\ 7)$$

provided there is only one facility existing in the radius L_r

It is evident from the foregoing formulation that the probability of the failure of the attacker's mission is a function of the plan area of the facility.

Hence, it is desirable to minimize the size of the facilities and disperse the same to an extent so as to reduce the probability of success of the attacker's mission A computer routine was written to solve the equation 3.2.1 6 to perform the parametric study to correlate the size of the facility and the probability of the failure of the attacker's mission. The study is preliminary in

nature as more classified military information which is secret in nature is required for a reliable situation However, it provides a basis to assess the reliability of such complexes

Results and discussion

The results plotted as shown in Fig 3 2 1 2 are based on following assumed capabilities of the attacker

CEPr   =100m
CEPe   =20m
Lr   =300m
N   =1

It is evident from the results that to have very high chances of survival the facilities should be made smaller in the size For the facility size of 30 sq m the probability of the failure of the attacker's mission is 98% which is quite reasonable The dispersal of the facilities should be more than the attacker's defined radius for a successful mission Therefore the important facilities should have dispersal of approximately 300m and less important facilities may have dispersal of 150 - 200m to keep the compactness of the complex.

3.2.2   Parametric studies for Optimal Depth of Burial
(Lower Limit)

As it is evident that the blast pressure decreases exponentially as the DOB increases [1] , whereas the overburden
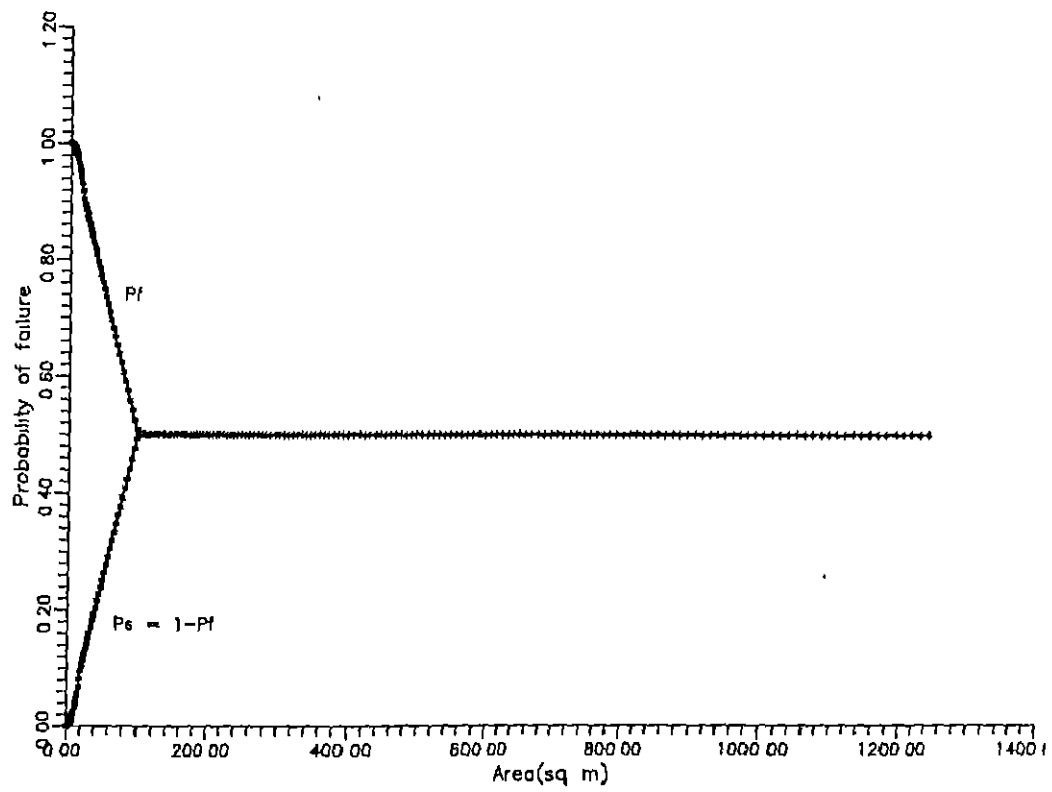
Fig 3 2 1 2   Probability of Failure vs Area of The Facility

pressure increase with DOB can be taken as linear for shallow depths. Therefore these two phenomenon combined together provide an optimum DOB for minimum over pressure.

In the present context the optimal depth of burial from minimum over pressure consideration for different ranges, height of burst and magnitudes of explosion, has been obtained by considering the soil arching effects and overburden pressure through following relations

The overburden pressure P_{over} increases linearly with depth by the following relation (Fig 3 2.2.1)

$$P_{over} = \gamma_s \cdot DOB \qquad . \qquad .(3.2.2.1)$$

where

γ_s Density of the soil taken into consideration

DOB   Depth of burial

The attenuation of Peak Over Pressure with DOB can be given by the following soil - arching equation which is based on a differential approach

$$\frac{P_{so}}{P_q} = \exp \left[\frac{-2 \ K_o \ (\tan\phi)(a + 1)bL^2}{aL^2} \right] \qquad (3.2 \ 2.2)$$

where

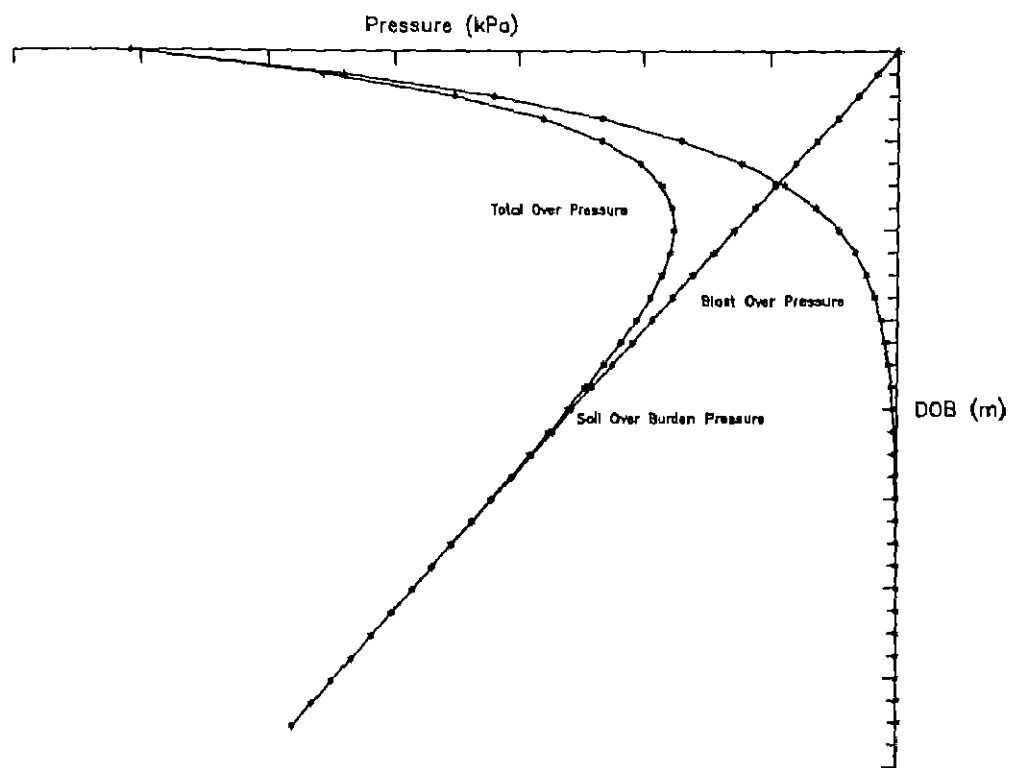P_{so} Peak over pressure and can be obtained by

Fig 3.2.2.1   Variation of Pressure with Depth of Burial

the analytical expression as given in Apex 'A'

P_q The attenuated over pressure at the DOB under consideration.

K_o Coefficient of earth pressure at rest

ϕ Angle of internal friction of the soil

a   Factor relating length of the structure to span

b   Factor relating DOB to the span

L   Length of the structure

Hence, the total Over pressure at any depth is given as,

$$P_{total}(DOB) = P_{ovr}(DOB) + p_q(DOB) \quad (3.2\ 2\ 3)$$

A computer program is written to solve the equation 3.2 2.3 to obtain the optimal depth of burial (for minimum total over pressure) for various ranges and heights of burst for parametric study The following parameters have been assumed constant in the program The values of these parameters are given as

$\gamma \quad = \quad 1.6\ kg/m^3$

$\phi \quad = \quad 20^0$

$K_o \quad = \quad 0.8$

$L \quad = \quad 6.0m$

$a \quad = \quad 2/3\ L$

$b \quad = \quad 2/3\ L$

Magnitude of Explosion $\quad = \quad$ 20kT

The results of the studies have been plotted as shown in Figs 3.2.2.2 ,3.2 2 3 and 3.2.2 4 for different feasible cases
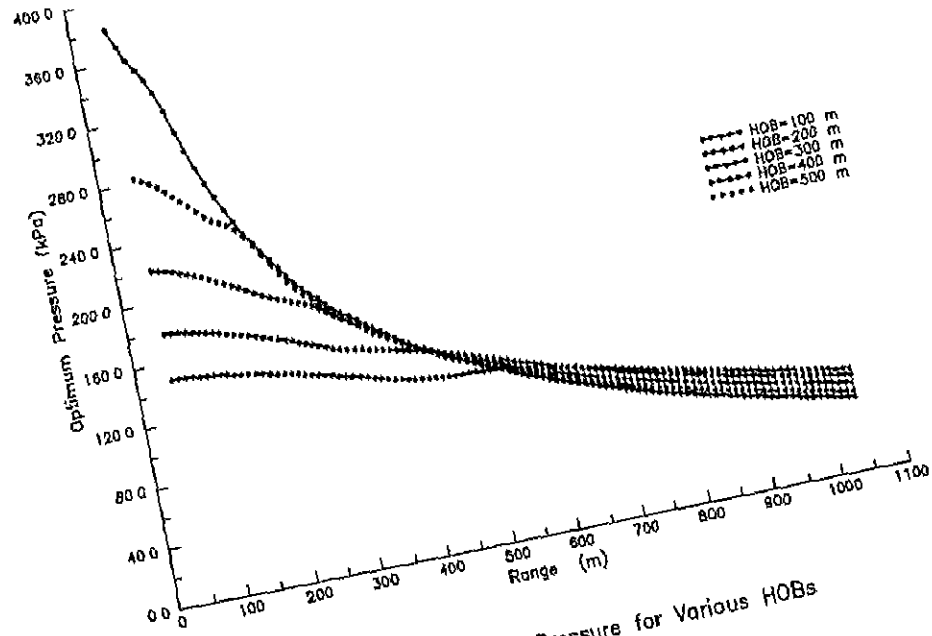
Fig 3 2 2 2 Range vs Optimal Pressure for Various HOBs
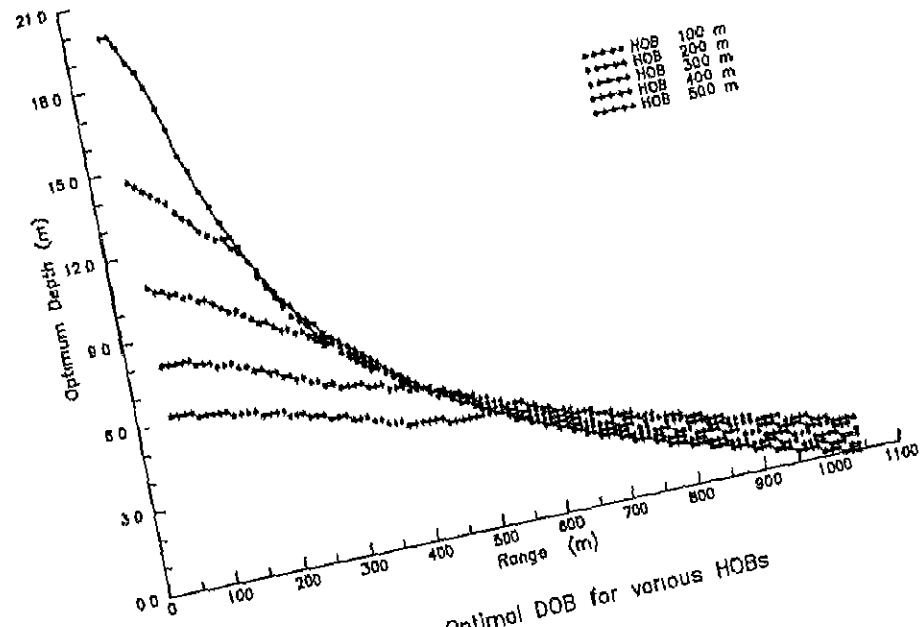

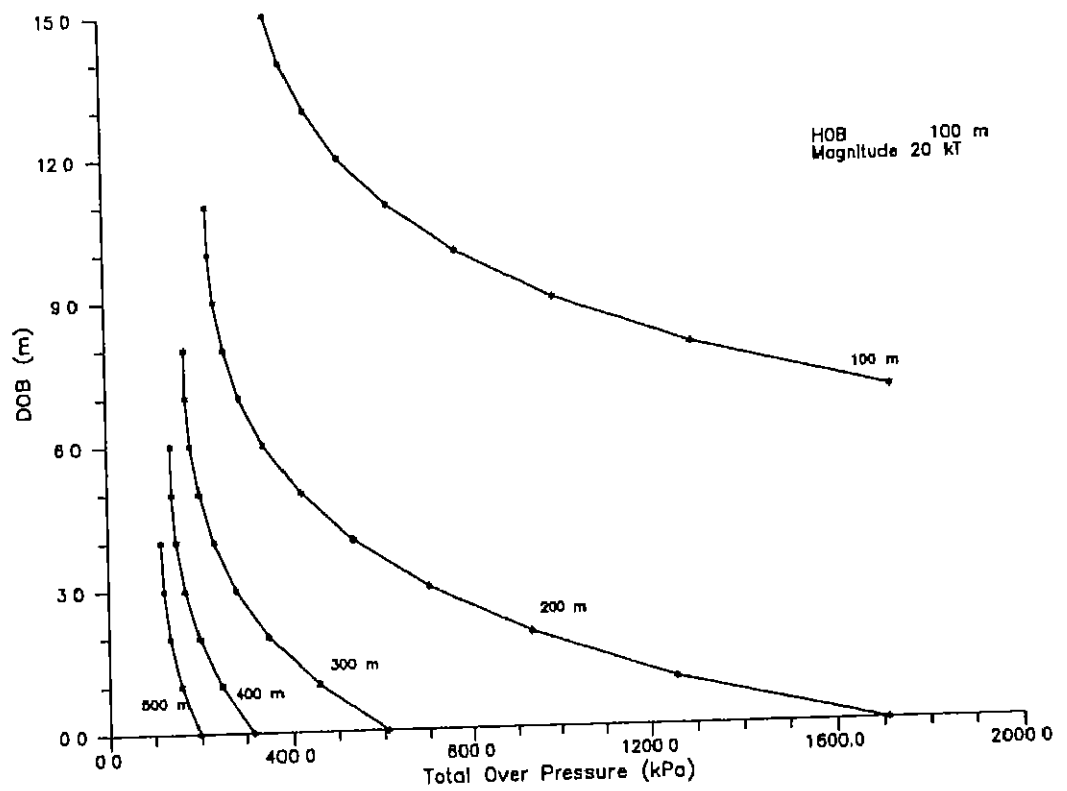Fig 3.2.2 3 Range vs Optimal DOB for various HOBs

Fig 3.2.2.4 Total Over Pressure vs Depth of Burial

and are discussed in succeeding paragraph.

Results and Discussion

The study is of general nature and provides the **lower limit** or **(maximum)** depth of the burial for shallow buried structures from total over pressure considerations

It is evident from the graphical results that for near surface bursts the values of optimal pressures and corresponding DOBs, for low ranges up to 500m are quite unstable These ranges should be avoided for construction. For HOBs up to 500m the optimal pressure and DOBs for 500-1000m range are more or less same and presents realistic values for design. Fig 3.2.2 4 can be taken as a design chart for obtaining correct DOB and corresponding pressure for precise calculations

3.2.3   Parametric studies for Optimal Depth of Burial (Upper Limit)

Another criteria for deciding the DOB for nuclear structures is radiation analysis. It is learnt from literature [1,3] that though the radiation is not a primary consideration for design but cannot be overlooked Therefore the upper limit of DOB is governed by radiation. In the present context upper limit has been obtained by keeping γ - radiation limit as 0.3 rem for personnel inside the citadel.

The principal approach adopted to obtain the **minimum** depth of burial for various ranges, HOB and Magnitude of explosion from

radiation consideration for different thickness is of the ordinary reinforced cement concrete is explained in Fig 3.2 3 1   The formulation of the problem is in the following

Nuclear Fission Data

1 kT	=	$2\ 6 \times 10^{25}$ Mev Energy
1 Fission	=	200 Mev
1 Fission	=	7 Mev release of energy
1 rad	=	0 01 J/Kg = 100 ergs/grm
1 Mev	=	1.6 E-6ergs

Assumptions

i)   Calculation of only primary and spontaneous flux is considered   It is presumed that if a person is able to sustain the initial concentrated dose, he/she would be able to survive under the reduced cumulative doses, due to   residual radiation

ii)   The personnel living inside the citadel are exposed to the worst γ ray flux.

iii)   For a common human being the   exposure   should be below 0.3 rem.

iv)   Residual radiation has not been considered   as it is an extremely small quantity

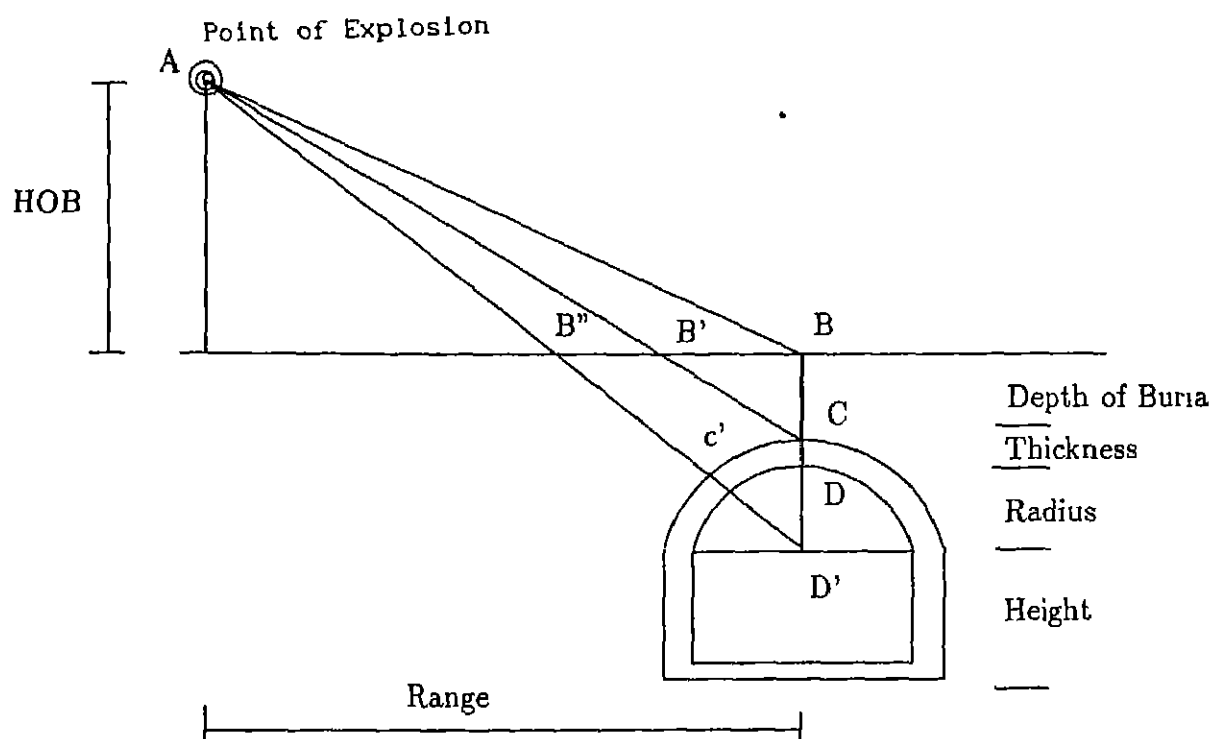v)   The neutron radiation has been taken as half of the γ ray equivalent, as   the   fission   and

Fig 3 2.3 1 Gamma Radiation Analysis

fusion bombs do not generate neutrons as primary weapon effects

Formulation

Let the flux at be A $= \phi_A$

Then

$$\Phi'_A = \frac{\phi_A}{4\pi y^2} \tag{3 2 3.1}$$

$$\phi_B = \frac{\phi_A}{4\pi AB^2} \tag{3 2 3 2}$$

$$\phi_C = \phi_B \, e^{-(\mu_a / \rho_s) \, BC} \tag{3.2.3.3}$$

$$\phi_D = \phi_c \cdot e^{-(\mu_a/\rho_c) \cdot t} \tag{3.2 3.4}$$

where

ϕ	γ - ray flux at any point
μ_a	Mass absorption coefficient
ρ_s	Density of the soil
ρ_a	Density of the concrete
BC	Direct thickness of the soil
t	Thickness of the concrete

The total number of γ - rays deposited in the human body inside the citadel can be expressed as (Worst possible case)

$$\gamma_{enh} = \phi_d \, A_h \tag{3 2.3.5}$$

where

A_h The average projected area of an average

human being

$$= \left[\frac{\phi_b}{4\pi y_1^2} \left(e^{-(\mu_a/\rho_s)} BC \right) \right] \left(e^{(-\mu_a/\rho_c).t} \right) * A_h$$

(3 2.3.6)

Hence, the energy deposited per unit weight of the average person(ergs/grm)

$$\gamma_{enh}/wt = \frac{(\gamma_{enh})}{W_h} . A * 1.6 \ E -6 \quad .. \quad (3.2 \ 3 \ 8)$$

When   quality factor(QF) = 1   then,

$$\gamma = \frac{(\gamma_{enh})}{W_h} A * 1 \ 6 \ E -6 \quad . . \quad (3 \ 2 \ 3 \ 9)$$

If the buildup factor for soil and concrete are B_s and B_c respectively as calculated by Taylor's method for 8 Mev γ ray energy   (which could be the most expected average energy of the γ ray emission in the nuclear explosion then,

$$B_s = A_s .e^{-\alpha_s \mu t} + (1 - A_s) e^{-\beta_s \mu t}$$

(3 2.3.10)

and

$$B_c = A_c \, e^{-\alpha_c \mu t} + (1 - A_c) \, e^{-\beta_c \mu t} \qquad (3\ 2\ 3\ 11)$$

As, Ac, αs, αc, βs, βc are Taylor's coefficients obtained from the Apex 'D'

Hence, the modified equations for flux after taking Buildup factor in to consideration are

$$\phi_{cm} = B_s \, \phi_c \qquad (3\ 2\ 3\ 12)$$

$$\phi_{dm} = B_c \cdot \phi_d \qquad (3.2\ 3\ 13)$$

A computer program has been written to solve above mentioned equations iteratively to obtain the minimum depth of burial for various ranges, height of bursts and thicknesses of the concrete

The results plotted are as shown in Figs 3 2 3.2, 3 2 3 3, 3 2.3 4 and 3 2.3 5. The results have been discussed in the succeeding paragraph

Results and Discussion

This parametric study provides the upper limit of the depth of burial. It is necessary to bury the structure up to this minimum limit to avoid the γ ray exposure, which may cause the harmful effects to the occupants of the complex.

This study revels that if DOB is more than 6m the structure is completely safe for near surface bursts. But DOBs of 2-6 m is
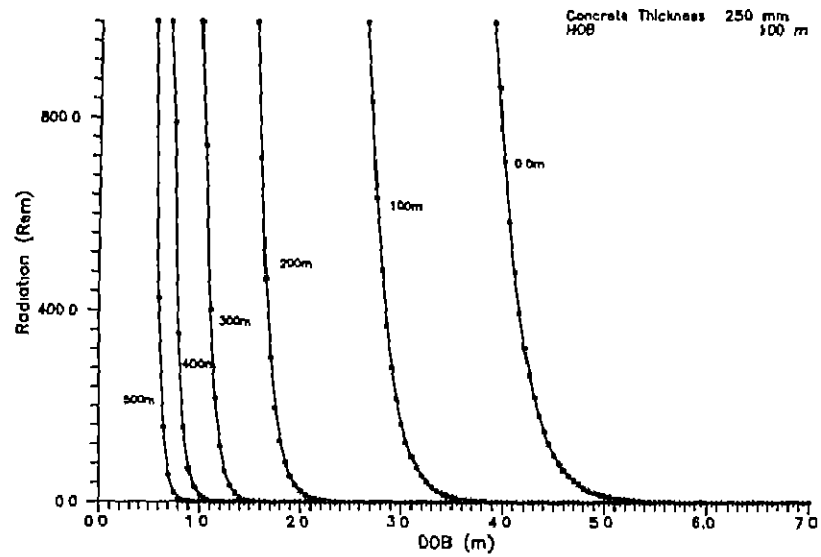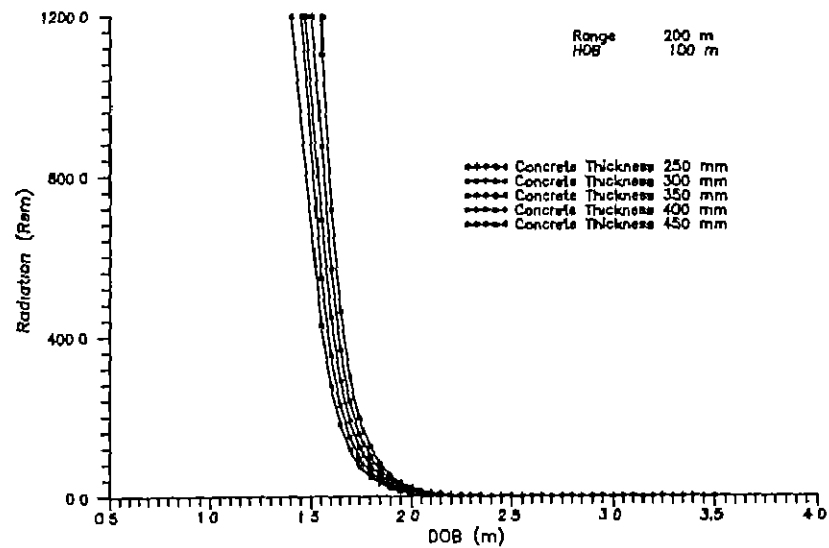
Fig 3 2 3 2 Radiation vs DOB for different Ranges

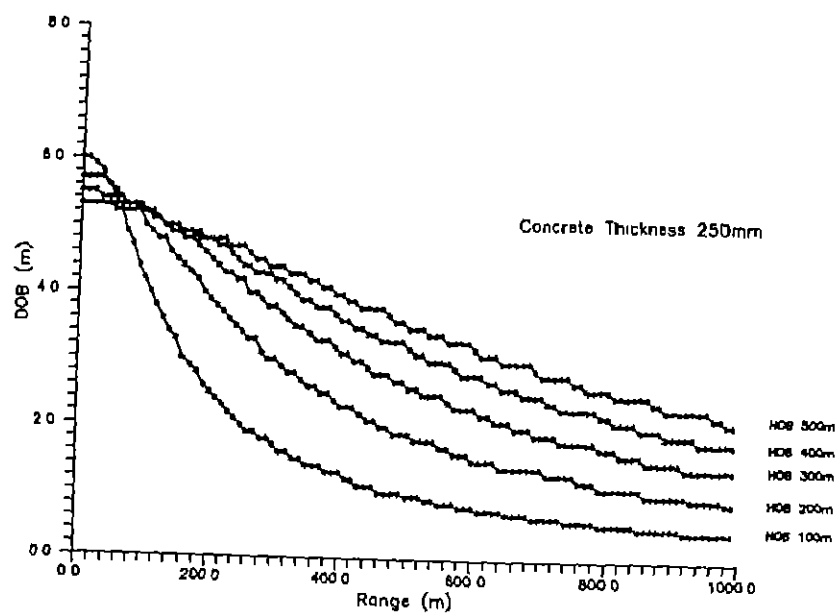Fig 3 2 3 3 Radiation vs DOB for Various thicknesses
of Concrete

Fig 3 2 3 4   Range vs Optimal DOB

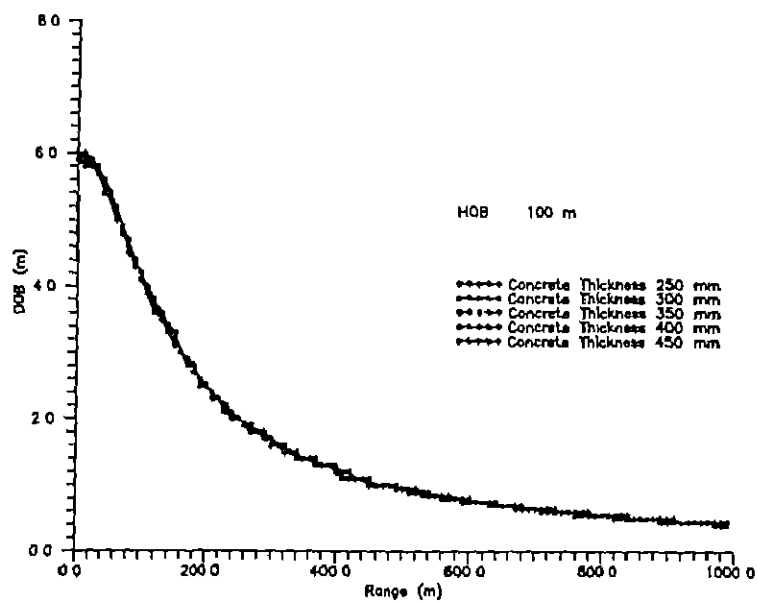Fig 3 2.3.5 Range vs Optimal DOB for Various
Thicknesses of Concrete

sufficient for most possible cases   The concrete is no better than soil as for as radiation absorption is considered and therefore minimum concrete thickness from over pressure considerations should be taken for the analysis   However to start the calculations for radiation a thickness of 250mm may be taken as standard

3.2.4   Parametric study for Thermal Radiation

Though the thermal radiation does not effect underground construction but it is important to ascertain the safe DOB from its effects   The parametric study performed in the following provides useful results on this aspect   The following assumptions have been made for the analysis

Assumptions

i)   Nuclear explosion source is considered   as a perfect black body.

ii)   No atmospheric attenuation is considered.

iii)   Only one third of the total energy of the explosion is associated with direct heat radiation

iv)   The test results of the Nevada test site, conducted by the United States Department of Defence (USDD) has been taken to obtain the pulse time and other specific details for formulation of the heat radiation.

Formulation

The fundamental approach adopted to calculate thermal radiation is as given in Fig 3 2 4 1

The approximate duration of the thermal pulse can be obtained in terms of t_{max} by the graphs as shown in the Fig 3.2 4 2

where
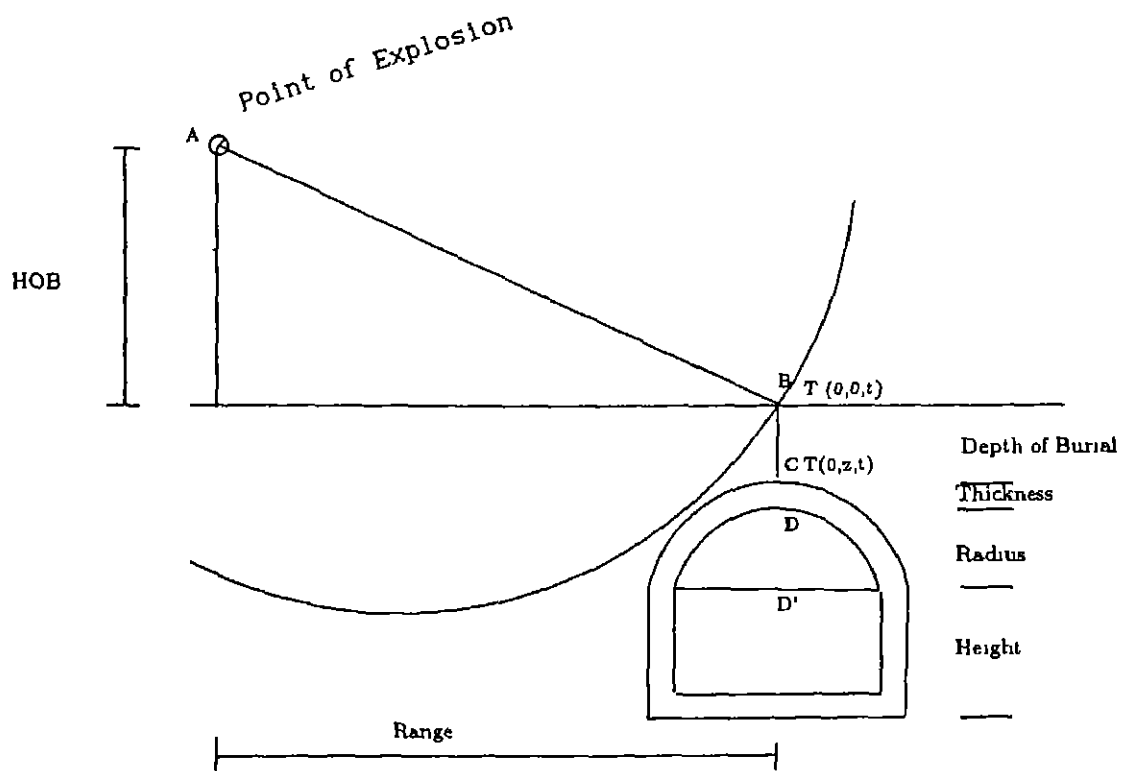
$$t_{max} = 0\ 032\ W^{1/2}\ s \qquad\qquad (3.2\ 3\ 1)$$

W weapon yield in kT

The total energy E_{tot} emitted in the pulse can be approximated as

$$E_{tot} = \frac{W}{3} \qquad\qquad (3\ 2.3\ 2)$$

If there is no atmospheric attenuation the thermal energy Q on the earth surface at a distance D from the point of the explosion can be given by the following relation. (Fig 3 2 4.1)

$$Q = \frac{E_{tot}}{4\ \pi\ D^2}\ e^{-kD} \qquad\qquad (3.2.3\ 3)$$

Fig 3.2.4.1   Thermal Radiation Analysis

where

k   Absorption coefficient averaged over the whole

spectrum of the wavelength

A   more   useful   formulation   for   thermal   energy

calculation can be given as

$$Q = \frac{f\ T\ W}{4\ \pi\ D^2} \qquad\qquad (3\ 2\ 3\ 4)$$

where

f   The fraction of the total yield in the form of

the radiation

T   *Transmittance*, a complex function of the

visibility, absorption and the distance   Its

value can be obtained from Fig 3 2 4 3

The temperature at the earth surface due to the pulse
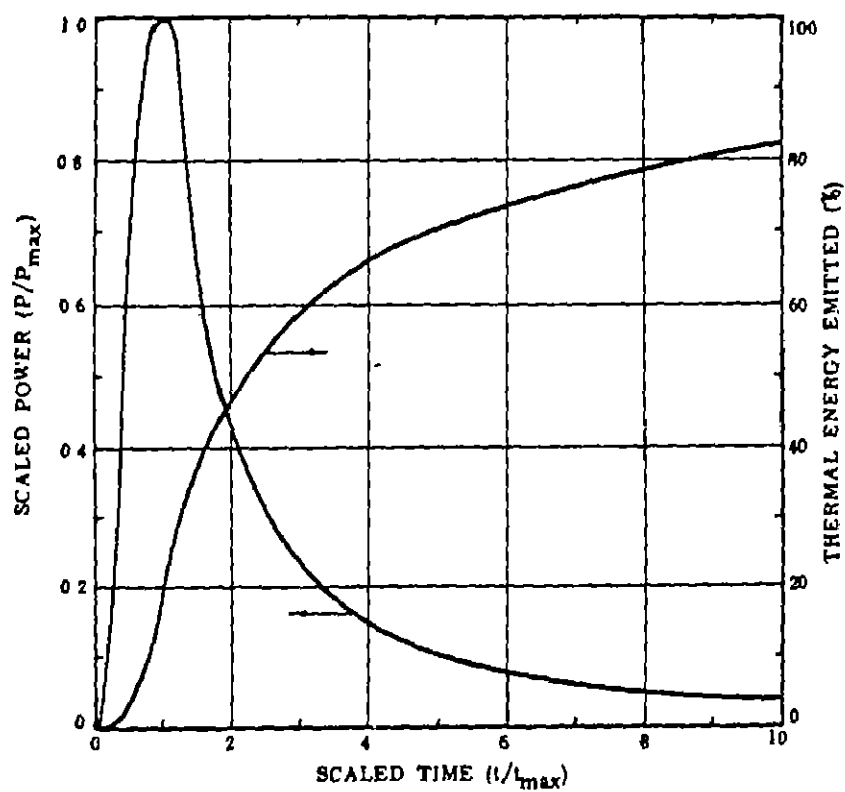
source is governed by the following relation

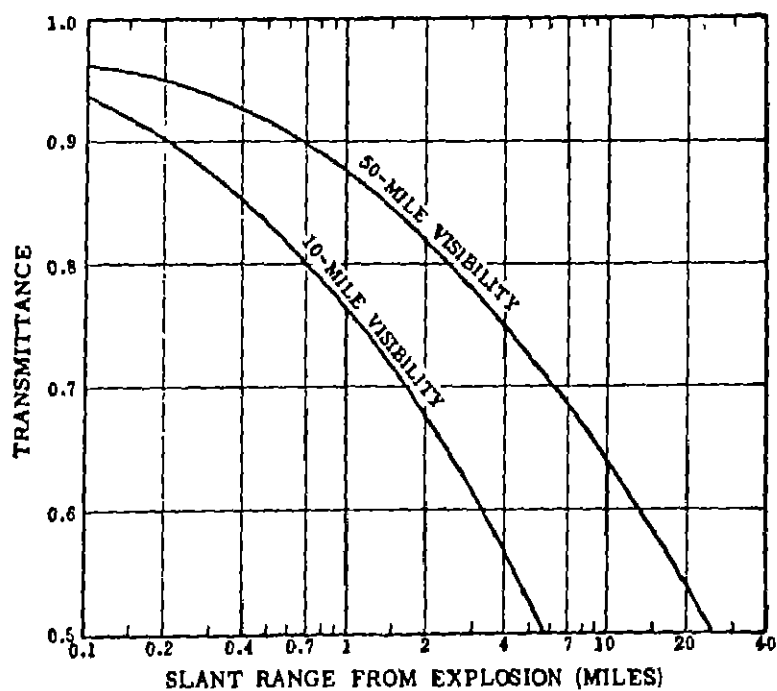Fig 3.2.4.2   Scaled Time for thermal Pulse

Fig 3.2.4.3   Transmittance

$$T(o,z,t) = \frac{2\ I\ (1-\varepsilon)}{\pi\ .A^2\ k}\left(\alpha\ t\right)^{1/2} . \left[\text{ierfc}\left(\frac{Z}{2(\alpha t)^{1/2}}\right) \right.$$

$$\left. - \text{ierfc}\left(\frac{(Z^2+A^2)}{2\ (\alpha t)^{1/2}}\right) \right]$$

(3 2 3 5)

where

I	Intensity of the incident thermal energy
A	Area of the source
ε	Emissivity of the material
k	Thermal conductivity
α	Thermal diffusivity of the material
t	Pulse time

The radiation of this transient temperature with time in atmosphere is given by Stefan – Boltzman law

$$\frac{\delta Tg}{\delta T} = \sigma\ \varepsilon\ \left[T_{g(t)}^4 - T_{(e)}^4\right]$$

(3 2 3 6)

where

σ	Stefan-Boltzman Constant (5.56 Watt/m^2)
ε	Emissivity of the soil
$T_{g(t)}$	Ground temperature in Kelvin at any time
T_e	Environment temperature
Z	Depth under consideration

The conduction at any depth is given by the principle of heat conduction through infinite solid medium and can be expressed by the following relation

$$\frac{T_B - T(z,t)}{T_s - T_e} = \text{erfc}\left(\frac{z}{2\,(\alpha t)^{1/2}}\right) \qquad (3\ 2\ 3\ 7)$$

where

T_s	Temperature at the ground surface at any time t in Kelvin
T_e	The environment temperature(K)
$T(z,t)$	Temperature at any depth z at any time t
α	Thermal diffusivity of the soil

A computer program is written and used to obtain the temperature histories at various depths using above mentioned formulation for different ranges & HOBs, for a specific composition of the soil (Apex 'E'). The program assumes the values of some of the parameters as given below

T	=	0.9
f	=	0.33
ε	=	0.93
k	=	0 13 W/m.deg
W	=	20kT

The Results obtained by varying the other parameters in the equations 3.2 3 6 and 3.2.3.7. The results obtained are plotted as shown in Figs 3.2.4.4, 3.2.4.5 and 3.2 4.6. These are discussed in following paragraph
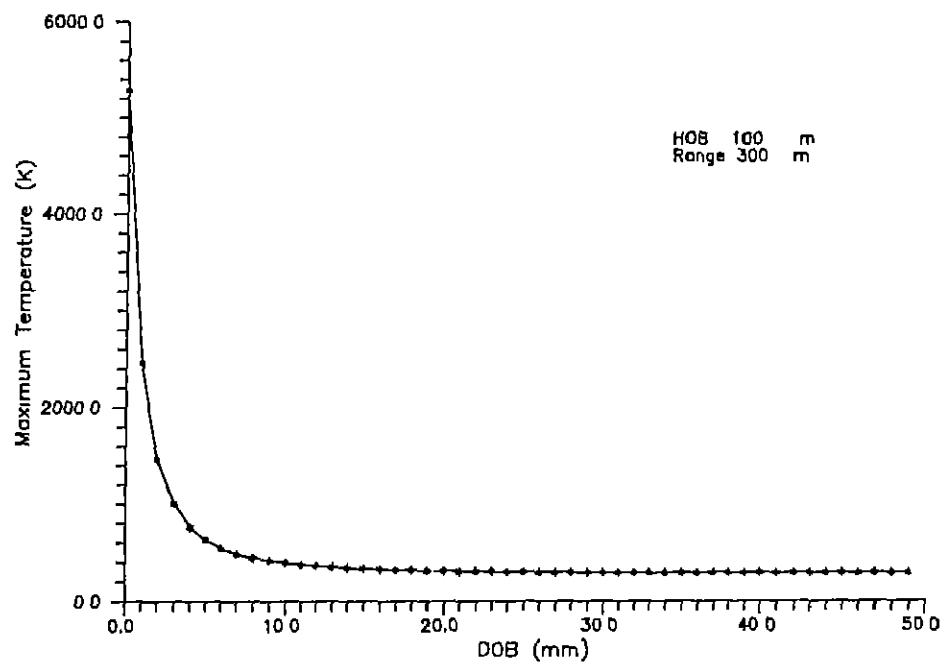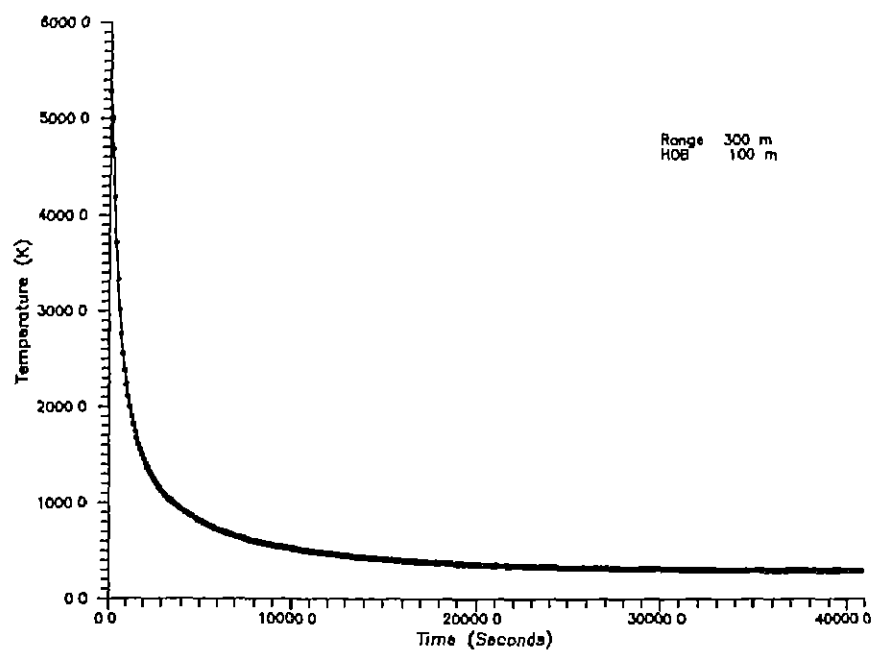
Fig 3 2.4.6   Maximum Temperature vs DOB

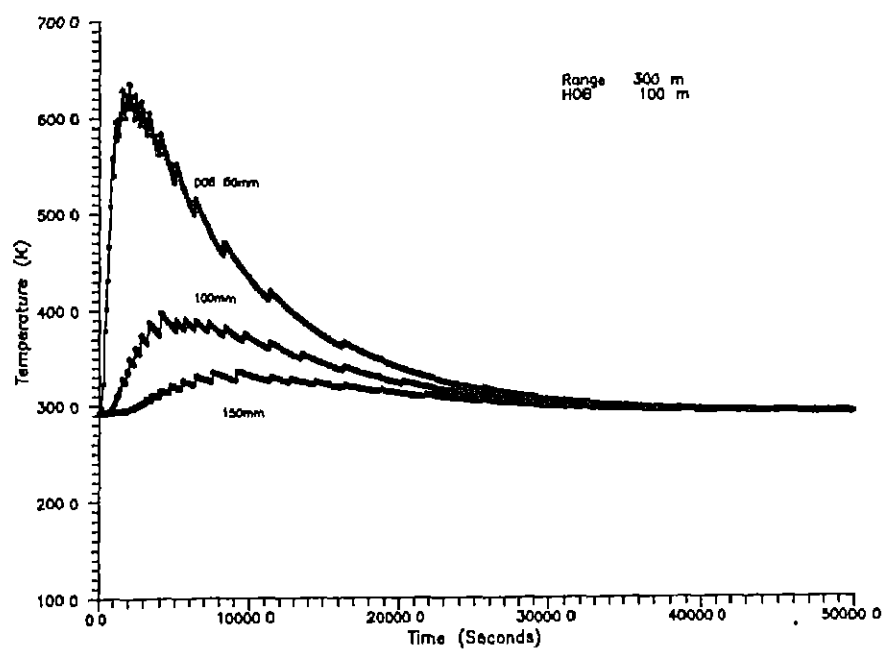Fig 3 2 4 4 Temperature vs Time at Ground Surface

Fig 3 2 4 5 Temperature vs Time for Various Depths

Results and Discussion

The maximum temperature at any depth may cause thermal expansion of the structural material and is of interest from stress analysis point of view

It is evident that for near surface bursts the temperature on the surface may be as high as 2000^0-3000^0c but it decays exponentially As the heat radiation from the top surface is faster than its conduction through soil layer Therefore the surface 1000mm below ground virtually remain unaffected As other forms of radiation requires more DOB for the optimum choice, therefore the thermal radiation is rarely a driver in design As a rough approximation it can be stated that the DOB more than 1 m is sufficient to protect against the heat radiation for near surface bursts

3.3   Pressure - Time History

the pressure time history at the ground surface at any distance from the point of explosion can be obtained from analytical expression as given in Apex 'B' This provides a scaled output for 1 kT of explosion   Therefore the output available needs to be de-scaled for the magnitudes of intrest.

The arrival time and the duration of the positive phase can also be interpreted from the above expression. The value of peak over pressure as input for this expression is calculated from the expression given in Apex 'A' The time histories at various depths depend on the soil and structure interaction with the blast wave As

a first approximation the time histories at any depth can be
calculated with following assumptions

Assumptions

i)   The load produced by ground shock on
        structures buried in a medium with a finite
        shear strength are influenced by structure
        medium interaction as the loaded structure
        deforms, besides by the effects of the
        propagating transient wave.

ii)   The reflected stress is relieved first by
        reflections from the concrete air interface at
        the bottom of the roof.

Formulation

With these assumptions the loading - time history at any
depth can be formulated as follows

The pressure - time history at any given slant range
from the point of explosion can be evaluated by the
analytical expression as given in Apex 'B'

For x >=xm and y <= 0.38

$$P_s(x,y,t) = P_s(r,z).(1+a).(b.v+c) \qquad (3.3.1)$$

and, for x < xm or y > 0.38

$$P_s(x,y,t) = P_s(r,z) \quad (b) \qquad\qquad (3\ 3\ 2)$$

where

$P_s(x,y,t)$ Pressure at any time t for any range r from the point of explosion

$P_s(r,z)$ Peak over pressure for any range r from the point of explosion and can be obtain by the analytical expression as given in Apex 'A'

the other variables are as explained in Apex 'B'

The stress at the roof surface at any depth without considering the soil arching relation can be obtained as

$$\sigma_r\ t) = P_s(x,y,t)\ (2 - t/t_d) \quad \text{for} \quad t <= t_d \qquad (3\ 3.3)$$

$$\sigma_r(t) = P_s(x,y,t) \qquad\qquad \text{for} \quad t < t_d \qquad\qquad (3\ 3\ 4)$$

If the soil arching is considered then

$$\sigma_r(t) = P_s(x,y,t).(2 - t/t_d) \quad \text{for} \quad t <= t_d$$

$$\sigma_r(t) = C_{\dot{a}}\ P_s(x,y,t) \qquad\qquad \text{for} \quad t < t_d \qquad (3.3.5)$$

The stress acting on the side of the shallow buried structure can be given as

$$\sigma_s(t) = K_o\ .\ P_s(x,y,t) \qquad\qquad (3\ 3.6)$$

If the soil - Arching is considered then

$$\sigma_s (t) = C_a \ K_o \ P_s(x,y,t) \qquad\qquad (3 \ 3 \ 7)$$

where

$$K_o = \frac{1 - Sin \ \phi}{1 + Sin\phi} \qquad\qquad (3 \ 3 \ 8)$$

This formulation provides vertical and horizontal pressure time histories acting on the roof and the side of the structure at the desired depth for shallow buried case   As the overburden pressure on the structure constantly acts on the structure, the total vertical σ_{rtotal} (t) and horizontal σ_{stotal} (t) histories can be obtained   as

$$\sigma_{rtotal}(t) \qquad = \ \sigma_r(t) \ + \ P_{viro} \qquad\qquad (3.3 \ 9)$$

$$\sigma_{stotal} \qquad = \ k_o \times \ \sigma_{rtotal}(t) \qquad\qquad (3.3 \ 10)$$

where

$$P_{viro} \qquad = \gamma \ . \ DOB$$

A computer program has been written to obtain the loading on the roof and the side of the buried structure for various ranges from the point of the explosion   The time-history obtained for a specific range (distance 300 m and HOB 100 m) and depths are shown in Figs 3.3.1. and 3.3.2 (a) and (b).   These have been further used for dynamic analysis of the proposed modules   In addition to the values
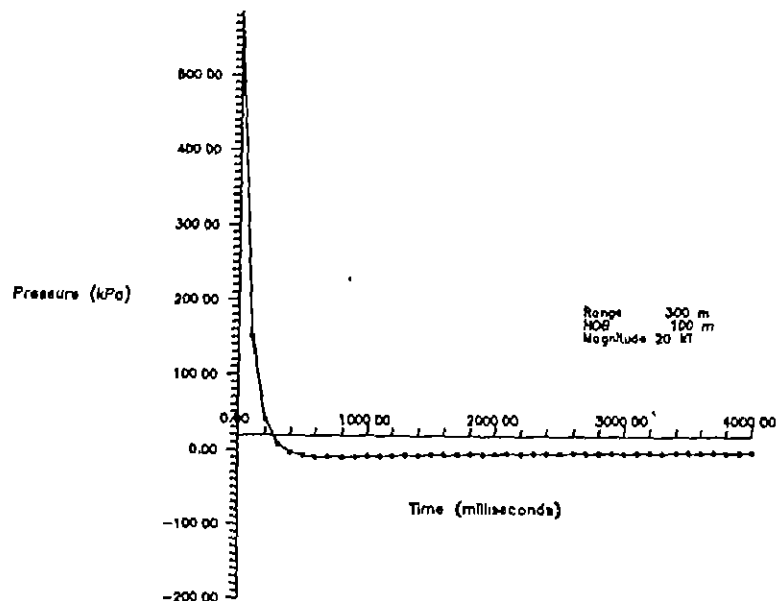
Fig 3.3.1 Surface Pressure — Time History
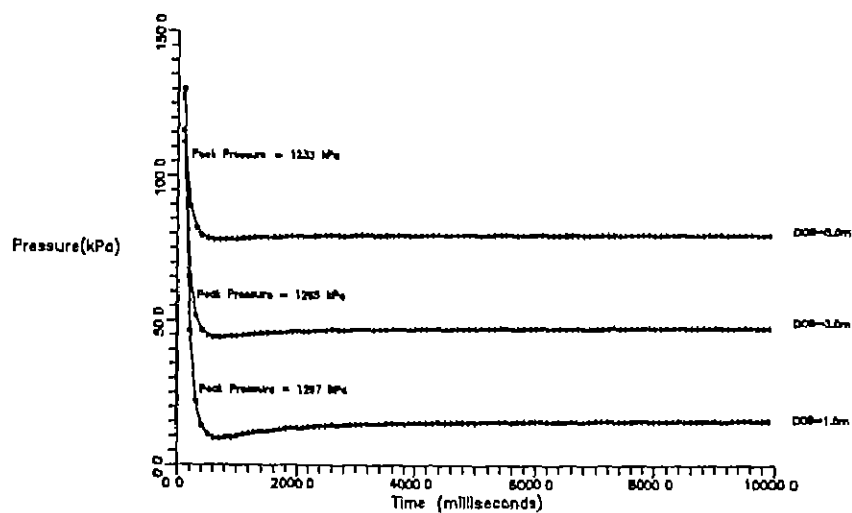

Fig 3.3.2 (a)   Vertical Pressure Time History at
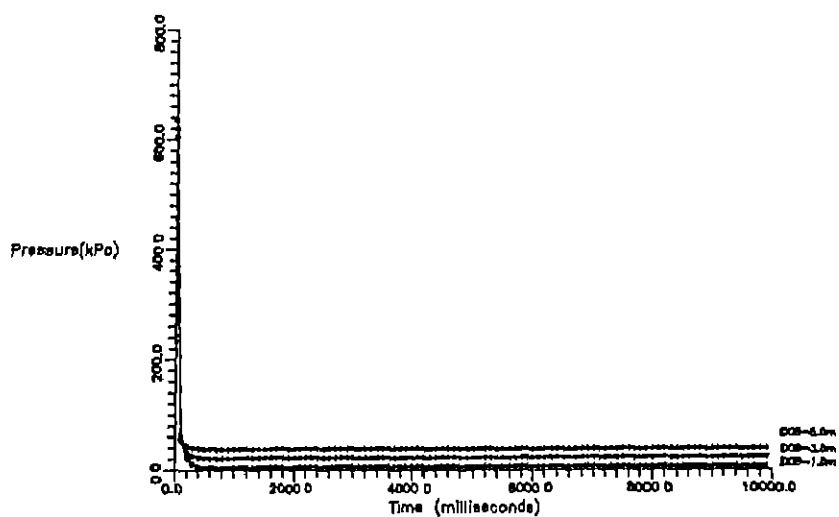Various Depths

Fig 3.3.2 (b)   Horizontal Pressure Time History at
Various Depths

ɔf parameters assumed in previous sections the program assumes the value of following parameters as

$$t_d = 12 \quad D / C$$

$C = 600$ m/s   Compression wave velocity

$D = 250$ mm   Thickness of the roof

3.4   Analysis

The static and dynamic analysis of one of the the principal module of the complex has been performed

The dimensions and other specifications of the module are as shown in Fig 3 4.1

The analysis has been performed for 20 kT explosion at 300m away at 100m HOB

M 20 concrete with density 24kN/m^3 has been used for analysis purpose   The other assumptions of parametric studies are valid for this analysis.

3.4.1   Load Modeling on the Principal Module

The load modeling of the principal module has been shown in Fig 3.4.2 (a) and (b) for static and dynamic analysis cases   The enveloped view of the module has been shown with loading on the elements.

3.4.2   Design Parameters

Based and the parametric studies performed in the previous sections, the design parameters obtained for the static analysis which are given in Table 3.4.2.1

Fig 3.4.1   Outline Diagram of the Principal Module

Fig 3.4.2 (a) Load Modeling of the Principal Module for

Static Analysis

Fig 3.4.2 (b) Load Modeling of the Principal Module for

Dynamic Analysis

Table 3.4.2.1   Design Parameters For a Specific Case

Range = 300m   HOB = 100m   Magnitude = 20 kT

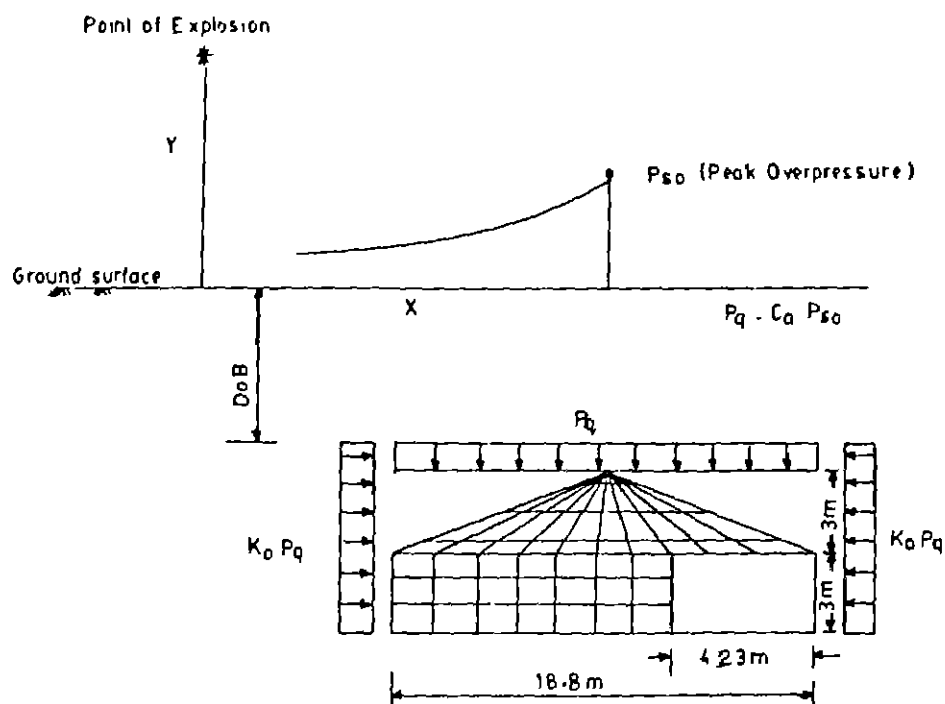| S.No	DOB (m)	Peak Over Pressure (kPa)	Over-Burden Pressure	γ- Radiation (Rem)	Thermal (K)
1	2 0	352 3	32 0	0 3	293
2	3 0	280 0	48 0	< 0 3	293
3	4.0	233 0	64 0	< 0 3	293
4	5.0	202	80 0	< 0.3	293

Similarly the vertical and horizontal time histories acting on the structure at 300m range at 4m depth are shown in Fig 3.3.2 (a) and (b). These histories have further been used for dynamic analysis

3.4 3   Finite Element Modeling

The suggested module of the complex has been modeled as thin shell elements of arbitrary geometry formed from four compatible triangles. The shell element uses the constant strain triangle. The central node is located at the average of the coordinates of the four nodes. The element has six degrees of freedom which are eliminated prior to the assembly, therefore the resulting quadrilateral element has four degrees of freedom i.e six degrees of freedom at each node

in the global coordinate system.

The bottom nodes are constrained in all the direction and other nodes have degrees of freedom in all the six directions

The openings in the module have been taken care of by providing different element type at the opening with negligible elastic modulus and the same thickness value to maintain the continuity and compatibility

The thermal radiation effects on the structure due to blast have been taken care of by providing the temperatures at nodes according to the results obtained by parametric studies of section 2 2 4

The Global and Elemental coordinate system are as shown in the Fig 3 4 3.1.

The finite element modeling of the module of the complex are as shown in Fig 3 4 3.2

A preprocessor was developed to provide input to SAP-IV for static analysis The loads on the shell elements act normal to the surface for analysis. The stresses and deflections of all the elements are recovered in output which is of interest for the design The following parametric studies are performed to obtain the desired mesh size for optimal results

3.4.3.1   Parametric Studies

The following parametric studies have been performed

i)   Stress on any arbitrary chosen element vs size
        of the mesh (Fig 3 4 3 3)

ii)   Bending moment per unit run on any arbitrary
        element vs size of the mesh (Fig 3 4.3.4)

iii)   Maximum stress vs size of the mesh

(a)   Element Coordinates

(b)   Global Coordinates

Fig 3.4.3.1   Elemental and Global Coordinates

Fig 3.4.3.2   Finite Element Modeling of the Principal Module

(Fig 3 4 3 5)

iv)   Maximum bending moment vs size of the mesh
        (Fig 3 4 3 6)

v)   Processor time vs number of elements
        (Fig 3 4 3 7)

Results and Discussion

The parametric studies performed above for optimal size of the mesh reveals that no of elements should be taken as 1600 - 2000 (250x250mm -200x200mm) for optimum results if the thickness of the model is uniform as 250mm. However, with increasing thicknesses at critical sections for stress reduction demands a fresh parametric study for the optimum results The element should be kept as square element.

3.4.4   Static Analysis

The parametric studies performed in the foregoing revealed that the openings and the joints of the shells are critical due to stress concentration   Even for the vertical pressure of 200 kPa the stresses on these sections exceeded the critical stresses almost by 200%.   Therefore the mesh size was readjusted with increasing thicknesses at these sections (ring beam at the joint of the shells)

The parametric studies were once again performed to obtain the desired results   It was found that the mesh size of 410mmx400mm (585 elements) provides the optimum stresses.

The static analysis performed is performed with this readjusted mesh for various load conditions and varying thicknesses The results obtained are as shown in Table 3 4 4 1.(a) and (b).

Fig 3 4.3 3 Stress on arbitrary element vs Number
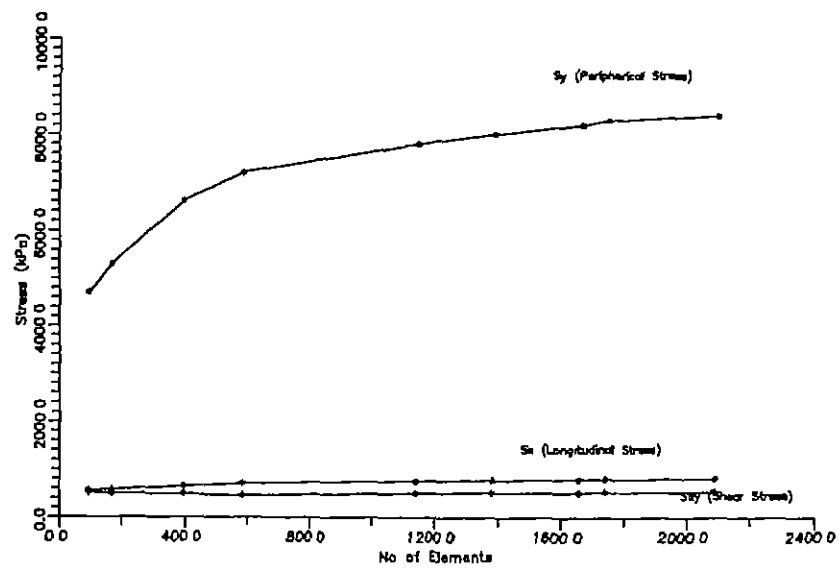of Elements
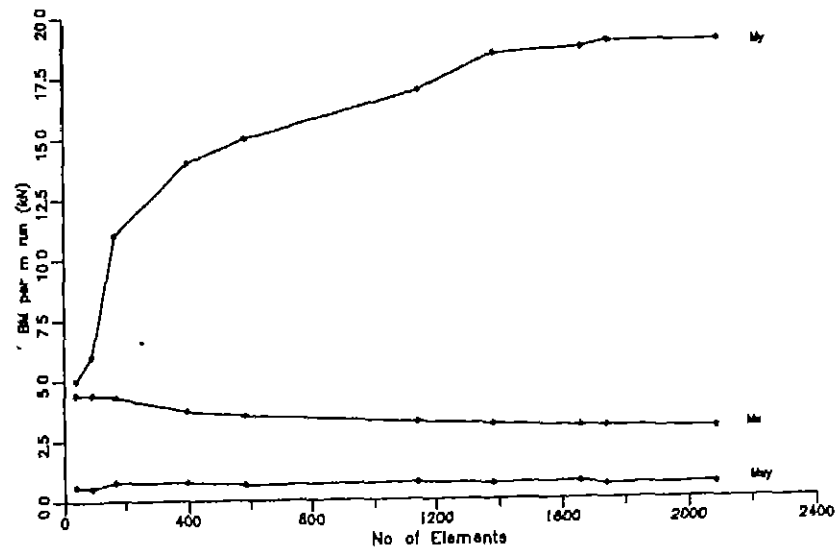

Fig 3 4 3 4 Bending moment on arbitrary element
vs Number of Elements

Fig 3 4 3 5   Maximum stress vs Number of Elements

Fig 3 4 3.6 Maximum Bending Moment vs Number
of Elements

Fig 3.4 3 7 Processor Time vs Number of Elements

Table 3.4.4.1 (a)   Results of Static Analysis

S	DOB (m)	Peak over pressure (kPa)	Thickness (mm)				Max Stresses (kPa)		
			Cylinder		Dome				
			Near opening (20^0)	Rest cyl	Ring beam	Rest dome	S_x	S_y	S_{xy}
1	2 0	352.3	600	300	400	200	0.15E4	0 36E4	0 63E3
2	2 0	352 3	500	250	300	150	0 20E4	0 41E4	0 67E3
3	2 0	352 3	400	200	200	100	0.27E4	0.52E4	0.10E4
4	3 0	280.0	600	300	400	200	0.13E4	0.32E4	0.62E3
5	3,0	280.0	500	250	300	150	0.16E4	0 36E4	0 64E3
6	3,0	280 0	400	200	200	100	0.21E4	0 45E4	0 79E3
7	4 0	233 0	600	300	400	200	0 13E4	0 30E4	0 63E3
8	4,0	233 0	500	250	300	150	0.13E4	0 33E4	0 64E3
9	4,0	233.0	400	200	200	100	0 18E4	0.40E4	0.67E3
10	5 0	202.0	600	300	400	200	0 13E4	0.29E4	0 63E3
11	5,0	202,0	500	250	300	150	0 13E4	0 31E4	0 64E3
12	5,0	202 0	400	200	200	100	0.15E4	0.37E4	0 67E3

Results and Discussion

The results obtained for various thicknesses of the module supports the fact that the critical sections are the openings (20^0 from the opening) and the joint of the shells.   Therefore additional thickness are required at the joint in form of ring beam and at the openings   The compressive stresses are the governing stresses for the design of the modules.   The maximum deflections in principle directions are as shown in Table 3.4.4 1 (b).

Table 3.4.4.1.(b)   Results of Static Analysis

S	DOB (m)	Peak over pre ssure (kPa)	Thickness (mm)				Max Deflections (mm)		
			Cylinder		Dome		X transl- ation	Y transl- ation	Z transl- ation
			Near opening (20^0)	Rest cyl	Ring beam	Rest dome			
1	2.0	352 3	600	300	400	200	0 22E-2	0 24E-2	0 22E-2
2	2 0	352.3	500	250	300	150	0 31E-2	0.30E-2	0 31E-2
3	2.0	352 3	400	200	200	100	0 52E-2	0 59E-2	0 50E-2
4	3.0	280 0	600	300	400	200	0 20E-2	0 21E-2	0 20E-2
5	3.0	280 0	500	250	300	150	0.27E-2	0 30E-2	0.27E-2
6	3 0	280.0	400	200	200	100	0.45E-2	0 52E-2	0 43E-2
7	4.0	233.0	600	300	400	200	0 18E-2	0 19E-2	0 18E-2
8	4.0	233.0	500	250	300	150	0 25E-2	0 27E-2	0 24E-2
9	4.0	233 0	400	200	200	100	0.40E-2	0.46E-2	0.39E-2
10	5.0	202.0	600	300	400	200	0.17E-2	0 18E-2	0 17E-2
11	5.0	202.0	500	250	300	150	0 23E-2	0 26E-2	0.23E-2
12	5.0	202 0	400	200	200	100	0.37E-2	0.43E-2	0.36E-2

3.4.5   Dynamic Analysis

As a first step to dynamic analysis natural frequencies and the mode shapes are calculated for three different specifications of the structure.

A preprocessor is developed to provide input to SAP-IV. The first and second frequencies obtained for various cases are as shown in Table 3.4.5.1.

Time History Analysis

For dynamic analysis the same module of the complex is loaded with two time histories acting simultaneously These histories are the same which were obtained in section 3.3 One of these acts vertically (X-direction) on spherical shell (top dome) for 90s The other acts horizontally (normal to the surface) on the cylindrical portion of the module for the same time The horizontal time history has further been resolved in global Y and Z directions for the loading on each element. The force on each element has been provided with the help of time multiplier function in SAP-IV

The time step has been chosen as 1 s. The damping has been assumed as 2%.

A preprocessor has been developed to provide above mentioned details as formatted input to SAP-IV for time integration.

The load modeling is as shown in Fig 3 4 2 (b)

The maximum stresses, deflections and the corresponding time are recovered as an output are given in Table 3.4.5 2.(a) and (b).

Table 3.4.5.1   Natural frequencies of the module   for various stiffnesses

S no	Thickness (mm)				Frequencies (Hz)	
	Near open (20°)	Rest cyli -nder	Ring beam	Rest cyli -nder	First	Second
1	600	400	400	200	0.3644E2	0.4361E2
2	500	300	300	150	0.3424E2	0 3842E2
3	400	200	200	100	0.2811E2	0 3099E2

Table 3.4.5 2 (a)   Results of Dynamic Analysis

S	DOB (m)	Peak over pre ssure (kPa)	Thickness (mm)				Max Stresses (kPa)		
			Cylinder		Dome		S_x	S_y	S_{xy}
			Near opening (20°)	Rest cyl	Ring beam	Rest dome			
1	3.0	280 0	600	300	400	200	951.6	1520.0	471 0
2	3 0	280 0	500	250	300	150	1189 0	2030 0	666 3
3	3.0	280 0	400	200	200	100	1641.0	3015 0	1094

Table 3.4.5.2 (b)   Results of Dynamic Analysis

S	DOB (m)	Peak over pre ssure (kPa)	Thickness (mm)				Max Deflections (mm)		
			Cylinder		Dome		X transl- ation (m)	Y transl- ation (m)	Z transl ation (m)
			Near opening (20°)	Rest cyl	Ring beam	Rest dome			
1	2.0	280 0	600	300	400	200	0.00142	0 00113	00134
2	2 0	280 0	500	250	300	150	0 00208	0 00189	00226
3	2.0	280.0	400	200	200	100	0.00370	0.00203	.00483

$$R_x = \frac{S_{xstatic}}{S_{xdynamic}} \cong 1\,3 \qquad R_y = \frac{S_{ystatic}}{S_{ydynamic}} \cong 1.7 \qquad R_{xy} = \frac{S_{xystatic}}{S_{xydynamic}} \cong 1\,0$$

where R_x, R_y R_{xy} are the ratios of static and dynamic stresses

Results and Discussion

The comparison of the results of static and dynamic analysis reveal the fact that the static analysis for blast load is over conservative. Therefore the dynamic analysis of these structures are recommended for economy in design of the complex   As the loading on these structures are one time measure, therefore

these structures should essentially remain safe from static overburden pressure

3.5 Design of Concrete Shells

Keeping in view the results of the analysis in the foregoing the design of the principal modules have been performed as per Indian Standard Codes of Practice [19,20 and 21]

3.5.1 Design

The moments of resistance of rectangular section based on the assumptions of 37.1 of IS·456(1962) for section without and with compression reinforcement is given in Apex 'E' of the code has been used as a basis of the design The elements have been assumed as rectangular sections

The element are checked for critical buckling stresses as per IS.2210(1962)   The procedure is rewritten in the succeeding paragraph.

3.5.2 Critical Buckling Stress

Instability in a shell may be caused by

- Local buckling in zones submitted to compressive stresses

- Brazier effect

-Combined effects of bending and torsion

Cylindrical Shells

The permissible buckling stress in a cylindrical shell may be calculated as follows

$$f_{perm} = \frac{0.25\ F_e}{1 + \dfrac{F_e}{F_{cr}}}$$ (3 5 2.1)

where

F_e Cube Strength of the concrete at 28 days

F_{cr} Critical stress determined in accordance with IS 2210(1962)

Buckling in Doubly Curved Shells

For spherical shells the permissible buckling load per unit area from consideration of elastic stability is given by the following relation

$$P_{perm} = 0.1\ \frac{E\ d^2}{R^2}$$ (3.5 2.2)

where

     E   Elastic modulus of concrete

     d   Thickness of shell and

     R   Radius of Curvature

3.5.3   Yield Criteria

The maximum moment at any corner of any element has been checked by assuming the elements as plate elements   Johnasen's plate theory is thus applied to check the ultimate moments in each element The principle approach adopted is given below

Let the reinforcement be placed in two orthogonal directions, one along radial X-axis and the other along the circumferential Y-axis of the shell. Since the reinforcement may not be same in both the directions, the corresponding plastic moments will also differ and the element will be orthotropic with regard to its ultimate strength.

Then the ultimate bending moments can be denoted by M_{pX} and M_{py} for the positive bending and M'_{pX} and $M'py$ for negative bending.

Yielding occurs when the bending moment on the cross section with angle α reaches a certain value. Refer Fig 3.5 3 1

Then according to Johansen's failure theory expressions for lower Y_L and upper yield Y_U curves can be given as

$$Y_L \qquad M_{p\alpha} = M_{pX}.cos^2\alpha + M_{py}.sin^2\alpha \qquad (3.5\ 3.1)$$

$$Y_U \qquad M_{p\alpha} = M'_{pX}\ cos^2\alpha + M'_{py}\ sin^2\alpha \qquad (3.5.3\ 2)$$

The yield condition in terms of the components M_x, M_y and M_{xy} is given

$$M_\alpha = M_x\ cos^2\alpha + M_y\ sin^2\alpha + M_{xy}.sin\ 2\alpha \qquad (3\ 5\ 3.3)$$

Then the condition to be checked is whether

$$M_{p\alpha} > M_{\alpha} \qquad\qquad (3\ 5\ 3\ 4)$$

A common computer program has been written to check the buckling stresses and permissible moments at all the corners of each element applying the above principle   As the buckling stress are the governing stresses therefore minimum reinforcement (16mm ϕ 250 mm c/c) has been provided in both the principle directions   The stresses obtained from the analysis are well within the permissible limits.
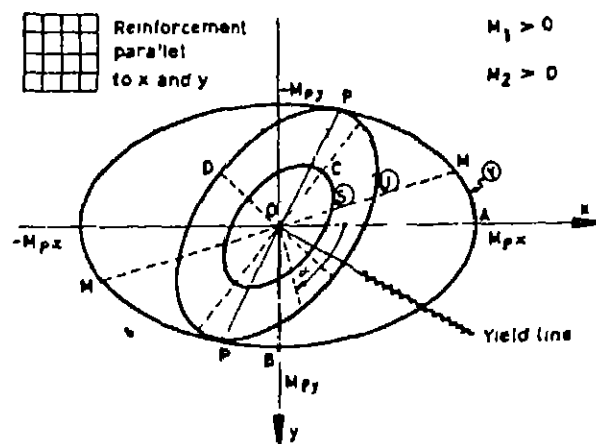
...

Fig 3.5.3.1   Yield Criteria for shell Elements

CHAPTER - IV

CONCLUSIONS

4.1 Suggested Algorithm

The algorithm suggested in section 3.1 incorporates all the effects of nuclear weapon which are governing forces for the design of the complex The planning, layout and design of the complex has been done as per this algorithm.

4.2 Parametric Studies

The parametric studies performed drive home the following points

i)   The probability of the failure of the attacker mission is a function of the dispersal of the facilities and the size of the modules Therefore the complex should be dispersed to the maximum and the dimensions of the facilities should be as small as possible

ii)   Parametric study performed for optimal depth of burial from blast pressure considerations reveals that burying structure deep in the ground is not only uneconomical but it has to designed for higher soil overburden pressure

iii)   The shallow buried structures are advantageous from blast, nuclear and thermal radiation considerations compare to above, mounded , surface flushed and deep buried structures .

iv)   The soil cover on the top of the structure is is more economical than the thickness of the concrete from radiation point of view.

v)   Upper limit of burial should be based on the radiation considerations.

vi)   Although the specialized concretes are available to combat the radiation but the ordinary RCC serves the purpose in present context

vii)   It is evident that the thermal radiation is rarely a driver in design but the upper layer of the soil up to one meter depth is susceptible to the thermal radiation   Therefore the structures should not be mounded or surface flushed

4.3   Static and Dynamic Analysis

i)   The static analysis carried out on the principal shell module supports the fact that the openings and the joints of the shells are critical from the stress concentration point of view. These should be

designed very carefully

ii)   The size of the mesh and its refinement with varying stiffness of the elements is important for desired results

iii)   The comparison of the static and dynamic stresses revals the fact that the static analysis for blast force is over conservative   Dynamic analysis should be resorted with taking soil arching into consideration As the analytical expression for the pressure-time history is approximate, the dynamic analysis with a factor of 1.5 is recommended.

4.4   Scope for future study

The design of structures to resist against nuclear weapon effects is a challenging field for civil engineers   The nations around the world have taken this aspect very seriously in recent years due to nuclear threats.

We may have to construct new structures or upgrade existing construction to cater for these threats which automatically opens new fields for research   The nonlinearity may be increased to obtain more accurate results for these effects. Also, the soil arching relations can be experimentally be found for realistic results.

CALCULATION OF AIR BLAST PEAK OVER PRESSURE

Given

     x   scaled range   in km/kT$^{1/3}$

     y   scaled Height of burst   in km/kT$^{1/3}$

     m   Magnitude of explosion   in kT

Then

$$r = \left(x^2 + y^2 \right)^{1/2}$$

$$z = y/x$$

Peak over pressure in kPa is given by

$$P_s(r,z) = \beta \left[\frac{10\ 47}{(\alpha\ r)^{a(z)}} + \frac{b(z)}{(\alpha\ r)^{f(z)}} + \frac{d(z)\ e(z)}{1 + f(z)\ (\alpha\ r)^{g(z)}} + h(z,r,y) \right]$$

in which

$$h(z,r,y) = \frac{-(64.67\ z^5 + 2905)}{1 + 441.4\ z^5} - \frac{1\ 389\ z}{1 + 49.03\ z^5} + \frac{8\ 808\ z^{1.5}}{1 + 154\ 5\ z^{3.5}} +$$

$$\frac{.0014(\alpha\ r)^2}{(1 - .158(\alpha.r) + 0486\ (\alpha.r)^{1\ 5} + 00128(\alpha.r)^2).(1 + 2\ y)}$$

where

$$\alpha = (0.3048)^{-1}, \text{ kft(km)}$$

$$\beta = (100/14.504), \text{ psi (kPa)}$$

$$a(z) = 1.22 \quad - \frac{3.908^2 z}{1 + 810\ 2\ z^5}$$

$$b(z) = 2.321 + \frac{6.195\ z^{18}}{1 + 1\ 113\ z^{18}} \quad - \frac{03831\ z^{17}}{1 + \ 02415\ z^{17}} \quad - \frac{6692}{1 + 4164\ \frac{8}{z}}$$

$$c(z) = 4\ 153 \quad - \frac{1\ 149\ z^{18}}{1 + 1.641\ z^{18}} \quad - \frac{1.1}{1 + 2\ 771\ z^{2.5}}$$

$$d(z) = -4.166 + \frac{25\ 76\ z^{1.75}}{1 + 1.382\ z^{18}} \quad - \frac{8\ 257\ z}{1 + 3\ 129\ z}$$

$$e(z) = 1 \ - \frac{.004642\ z^{18}}{1 + .003886\ z^{18}}$$

$$f(z) = .6096 + \frac{2.879\ z^{9\ 25}}{1 + 2\ 359\ z^{14.5}} \quad - \frac{17\ 25\ z^2}{1 + 71.66\ \frac{3}{z}}$$

$$g(z)^2 = 1\ 83 + \frac{5.361\ z}{1 + .3139\ z^6}$$

ANALYTICAL EXPRESSION FOR PRESSURE - TIME HISTORY

For $x >= xm$ and $y <= 0\ 38$

$$P_s(x,y,t) = p_s(r,z) \cdot (1 + a)\ (b\ v + c)\left(\frac{100}{14.504}\right) kPa$$

For $x < xm$ or $y > 0\ 38$

$$P_s(x,y,t) = p_s(r,z) \cdot (b)\left(\frac{100}{14\ 504}\right) kPa$$

Where

     x scaled ground range, $kft/kT^{1/3}$

     y scaled height of burst, $kft/kT^{1/3}$

     t scaled time $msec/kT^{1/3}$

$$a = (d - 1) \cdot \left(1 - \frac{e^{20}}{1 + e^{20}}\right)$$

$$d = 0.27 + \frac{58300y^2}{26667 + 1000000y^2} + 0\ 27\ (e) - \left(0.5 - \frac{0\ 583000y^2}{26667 + 1000000y^2}\right)e^5$$

$$e = \frac{\left|\ x - xm\ \right|}{\left|\ xe - xm\ \right|}$$

$$xm = \frac{170\ y}{1 + 337\ y^{0\ 25}} + 0.91\ y^{2.5}$$

$$xe = \frac{3\ 039}{1 + 6.7\ y}$$

$$b = \left[f \left(\frac{t_a}{t} \right)^g + (1-f) \left(\frac{t_a}{t} \right)^h \right] \left[1 - \frac{(t-t_a)}{dp} \right]$$

$$t_a = u \qquad\qquad \text{for } x < x_m$$

$$t_a = u \frac{x_m}{x} + w \left(1 - \frac{x_m}{x} \right) \qquad \text{for } x \geq x_m$$

$$u = \frac{(0\ 543 - 21.8r + 386r^2 + 2383r^3)r^8}{2\ 99\ 10^{-14} - 1.91\ 10^{-10}r^2 + 1\ 032\ 10^{-6}r^4 - 4.43\ 10^{-5}r^6 + (1\ 632 + 2\ 629 + 2\ 69r^2)r^8}$$

$$w = \frac{(1\ 086 - 34\ 605r + 486\ 3r^2 + 2383r^3)r^8}{3.0137\ 10^{-13} - 1.2128.10^{-9}r^2 + 4.128\ 10^{-6}r^4 - 1.116\ 10^{-5}r^6 + (1\ 632 + 2\ 629r + 2.69r^2)r^8}$$

$$dp = \left(\frac{1640700 + 24629\ t_a + 416\ 15\ t_a^2}{10,880 + 619\ 76\ t_a + t_a^2} \right) * \ \dots$$

$$\left[\left(0.4 + \frac{0.001204\ t_a^{1.5}}{1 + 0.001559\ t_a^{1.5}} \right) + \left(0.0426 + \frac{0\ 5486\ t_a^{0.25}}{1 + 0\ 000357\ t_a^{1.5}} \right) (s) \right]$$

$$s = 1 - \frac{1.1.10^{10}y^7}{1 + 1.1.10^{10}y^7} - \left(\frac{2.441\ 10^{-8}y^2}{1 + 9\ 10^{10}y^7} \right) \left(\frac{1}{4\ 41.10^{-11} + x^{10}} \right)$$

$$f = \left(\frac{0\ 01477t_a^{75}}{1 + 0\ 005836t_a} + \frac{7\ 402\ 10^{-5}t_a^{2.5}}{1 + 1.429.10^{-8}t_a^{4.74}} - 0\ 216 \right) . (s) +$$

$$0.7076 - \frac{3.077.10^{-5}t_a^3}{1 + 4.367\ 10^{-5}t_a^3}$$

$$g = 10.0 + \left(77.58 - \frac{64.99t_a^{0.125}}{1 + 0\ 04348t_a^{0.5}} \right) . (s)$$

$$h = 2\ 753 + \frac{0.05601ta}{1+1.473\ 10^{-9}ta^5} + \left(\frac{0\ 01769ta}{1 + 3\ 207\ 10^{10}\ t_a^{4\ 25}} - \right.$$

$$\left. \frac{0\ 03209ta^{1.25}}{1 + 9.914.10^{-8}\ ta^4} - 1.6 \right)\ (s)$$

$$v = 1 + \left(\frac{3\ 28\ 10^{11}y^6}{1+1\ 5.10^{12}y^{6\ 75}} \right) \left(\frac{ga^3}{6\ 13+ga^3} \right) \left(\frac{1}{1\ +\ 9\ 23\ e^2} \right)$$

$$c = \left[\frac{1.04 - \left(\frac{240.9x^4}{1+\ 231.7x^4} \right)(ga)^7}{(1+a)\ [1+0\ 923(ga)^{8\ 5}]} \right] \cdot \left[\frac{2.3.10^{13}y^9}{1\ +\ 2.3.10^{13}y^9} \right] \times$$

$$\left[1 - \left(\frac{(t\ -\ ta)}{dp} \right)^8 \right]$$

$$ga = \frac{t\ -\ ta}{dp}$$

$$dt = 474.2.y.(\ x-xm)^{1\ 25}$$

Here

xm	An approximation to the begining of mach reflection region
xe	Approximation to the points in the double peak region where the peaks are equal.
dt	Time sepration between the first & second peak
d	Ratio of the first peak to second peak
ta	Approximation to the shock arrival time
dp	Approximation to the duration of the positive phase.

Clinical Effects of Ionizing Radiation Doses

Effect/Phase (1)	DOSE/RANGE					
	0 to 100 rems —subclinical range (2)	100 to 1,000 Rems— Therapeutic Range			Over 1,000 Rems— Lethal Range	
		100 to 200 rems— clinical surveillance (3)	200 to 600 rems— therapy effective (4)	600 to 1,000 rems— therapy promising (5)	1,000 to 5,000 rems— therapy palliative (6)	Over 5,000 rems— therapy palliative (7)
Incidence of vomiting	None	100 rems Infrequent 200 rems common	300 rems 100%	100%	100%	100%
Initial phase Onset Duration	— —	3 to 6 hr ≤ 1 day	½ to 6 hr 1 to 2 days	¼ to ½ hr ≤ 2 days	5 to 30 min ≤ 1 day	Almost immediately[b]
Latent phase Onset Duration	— —	≤ 1 day ≤ 2 wk	1 to 2 days 1 to 4 wk	≤ 2 days 5 to 10 days	≤ 1 day[a] 0 to 7 days[a]	Almost immediately[b]
Final phase Onset Duration	— —	10 to 14 days 4 wk	1 to 4 wk 1 to 8 wk	5 to 10 days 1 to 4 wk	0 to 10 days 2 to 10 days	Almost immediately[b]
Leading organ	Hematopoietic tissue				Gastrointestinal tract	Central nervous system
Characteristic signs	None below 50 rems	Moderate leukopenia	Severe leukopenia; purpura, hemorrhage, infection Epilation above 300 rems		Diarrhea; fever, disturbance of electrolyte balance	Convulsions, tremor, ataxia, lethargy
Critical period postexposure	—	—	1 to 6 wk		2 to 14 days	1 to 48 hr
Therapy	Reassurance	Reassurance, hematologic surveillance	Blood trans- fusion, anti- biotics	Consider bone marrow trans- plantation	Maintenance of electrolyte balance	Sedatives
Prognosis	Excellent	Excellent	Guarded	Guarded	Hopeless	
Convalescent period Incidence of death	None None	Several wk None	1 to 12 mo 0 to 90%	Long 90 to 100%	— 100%	
Death occurs within	—	—	2 to 12 wk	1 to 6 wk	2 to 14 days	< 1 day to 2 days
Cause of death	—	—	Hemorrhage, infection		Circulatory collapse	Respiratory failure, brain edema

[a] At the higher doses within this range there may be no latent phase
[b] Initial phase merges into final phase, death usually occurring from a few hours to about 2 days, this chronology is possibly interrupted by a very short latent phase.

TAYLOR'S METHOD FOR CALCULATION OF BUILDUP FACTORS

Taylor's formula for calculation of buildup factor is

$$B = A.e^{-\alpha\mu t} + (1 - A)e^{-\beta\mu t}$$

Where values of A, α, β for exposure buildup factor data for ordinary Concrete & soil of the composition given in Apex 'E' are given in the Tables below

For Ordinary Concrete

Photon Energy Mev	A	α	β
0.5	12.5	-0 110	0 010
1 0	10.0	-0.088	0 029
2.0	6.3	-0 069	0.058
4.0	3.9	-0 059	0 079
6 0	3 1	-0 059	0 083
8 0	2.7	-0 056	0 086
10.0	2 6	-0.050	0 084

For soil

0.5	70.0	0.0754	-0.0471
1.0	20 6	0.0653	0.0224
2.0	9.67	0.0538	0.0599
4.0	6.5	0 0388	0.0690
6.0	5.2	0.0357	0.0675
8.0	3.5	0.0421	0.0920

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